Test 2: Exponents and surds [51]

Question 1

1.1 Simplify each of the following

$$2.1.1 \quad \frac{(3x)^{-2}}{3x^{-3}} \tag{3}$$

$$2.1.2 \quad \frac{x^{-1} + y^{-1}}{x^{-1}y - y^{-1}x} \tag{5}$$

$$2.1.3 \quad \sqrt{108x^{12}} + \sqrt{243x^{12}} \tag{3}$$

2.2 Solve for
$$x: 2^{3x-6} = \sqrt{8}$$
 (3)

1.3 Solve for x if

$$1.3.1 \quad 9^{x^2+x} = 27^{x+1} \tag{5}$$

1.3.2
$$2^{x+1} + 2^{x+2} = 48$$
 (5)

$$1.3.3 \quad 3^{2x} - 3.3^x = -2 \tag{5}$$

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Question 2

2.1 Simplify each of the following:

$$2.1.1 \ \frac{x^{\frac{1}{3}} \cdot x^{\frac{1}{4}}}{x^{\frac{1}{6}}} \tag{3}$$

$$2.1.2 \ \sqrt{128x^6} + \sqrt{98x^6} \tag{3}$$

2.1.3 Show that
$$\frac{\sqrt{x}}{x} + \frac{y}{\sqrt{x}}$$
 can be written as $\frac{\sqrt{x}(1+y)}{x}$ (4)

2.2 Simplify:

$$2.2.1 \quad \frac{3\sqrt{18} - \sqrt{50}}{2\sqrt{72}} \tag{4}$$

$$2.2.2 \quad \frac{2\sqrt{18} - \sqrt{32}}{\sqrt{8} + \sqrt{2}} \tag{4}$$

$$2.2.3 \quad \frac{\sqrt{75} - \sqrt{18}}{\sqrt{12}} \tag{4}$$
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