



PHYSICAL SCIENCES

MATERIAL FOR GRADE 12

SECOND TERM

WORK-ENERGY THEOREM

MEMORANDA

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QUESTION 7/VRAAG 7

7.1 $200 \times 1\,000 = 2 \times 10^5 \text{ kg} \checkmark$ [12.2.3] (1)

7.2 $E_{ki} + E_{pi} = E_{kf} + E_{pf} \checkmark$ or/of $E_{\text{mech } i} = E_{\text{mech } f}$ or/of $\Delta E_p = \Delta E_k$
 $0 + mgh_i = E_{kf} + 0$
 $0 + (2 \times 10^5)(9,8)(150) \checkmark = E_{kf} + 0 \checkmark$
 $\therefore E_{kf} = 2,94 \times 10^8 \text{ J} \checkmark$

OR/OF

$$W_{\text{net}} = \Delta E_k$$

$$F \cos \theta \Delta y = E_{kf} - E_{ki} \checkmark$$

$$(200\,000)(9,8)(\cos 0^\circ)(150) \checkmark = E_{kf} - 0 \checkmark$$

$$\therefore E_{kf} = 2,94 \times 10^8 \text{ J} \checkmark$$
 [12.2.3] (4)

7.3 $E_{kf} = \frac{1}{2}mv_f^2 \checkmark$
 $2,94 \times 10^8 \text{ J} = \frac{1}{2}(2 \times 10^5)v_f^2 \checkmark$
 $v_f = 54,22 \text{ m} \cdot \text{s}^{-1} \checkmark$ [12.2.3] (3)

7.4 $P = \frac{85}{100} \times \frac{W}{\Delta t} = \frac{85}{100} \times \frac{2,94 \times 10^8}{1} \checkmark$
 $= 2,499 \times 10^8 \text{ W} \checkmark$ Accept/Aanvaar $2,5 \times 10^8 \text{ W}$

OR/OF

$$E_k(\text{effective/effektief}) = \frac{85}{100} \times 2,94 \times 10^8 \checkmark = 2,499 \times 10^8 \text{ J}$$

$$P = \frac{W}{\Delta t} = 2,499 \times 10^8 \text{ W} \checkmark$$
 Accept/Aanvaar $2,5 \times 10^8 \text{ W}$ [12.2.3] (2)

7.5 Converted to sound / heat in turbine / other forms of energy. $\checkmark$
Omgeskakel na klank / hitte in die turbine / ander vorms van energie [12.2.3] (1)
[11]

QUESTION 6/VRAAG 6

6.1.1 $W_{\text{net}} = \Delta E_p + \Delta E_k \checkmark$
 $\therefore W_{\text{net}} = (mgh_f - mgh_i) + (\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2)$
 $\therefore 7 \times 10^5 \checkmark - 8,5 \times 10^4 \checkmark = 10\,000(9,8)(h_f - 0) \checkmark + 0 \checkmark$
 $\therefore 6,15 \times 10^5 = 10\,000(9,8)h_f$
 $\therefore h_f = 6,28 \text{ m} \checkmark$

OR/OF

Useful work done = gain in $E_p \checkmark = mgh \checkmark$
Bruikbare arbeid verrig = wins aan $E_p \checkmark = mgh \checkmark$
 $\therefore 7 \times 10^5 \checkmark - 8,5 \times 10^4 \checkmark = 10\,000(9,8)h \checkmark$
 $\therefore 6,15 \times 10^5 = 10\,000(9,8)h_f$
 $\therefore h = 6,28 \text{ m} \checkmark$

[12.1.3] (6)

6.1.2 $W = F \Delta x \cos \theta \checkmark$
 $\therefore 7 \times 10^5 = F(23)(1) \checkmark$
 $\therefore F = 3,04 \times 10^4 \text{ N} \checkmark$

$P = Fv \checkmark$
 $= (3,04 \times 10^4) \left(\frac{20\,000}{60 \times 60} \right) \checkmark$
 $= 1,6 \times 10^5 \text{ W} \checkmark$

[12.1.3] (6)

6.2 Any TWO/Enige TWEE:
 Surface must provide sufficient friction like sand $\checkmark$
 Must be long enough for vehicle to stop. $\checkmark$
Oppervlak moet genoeg wrywing lewer soos sand $\checkmark$
Moet lank genoeg wees om die voertuig tot stilstand te bring $\checkmark$

(2)
 [12.3.2] **[14]**

QUESTION 5/VRAAG 5

5.1 0 (N)/Zero/nul ✓
no acceleration/constant velocity ✓
geen versnelling/konstante snelheid [12.2.3] (2)

5.2 0 (J)/Zero/nul ✓ [12.2.3] (1)

5.3.1

Option 1/Opsie 1:

$$\begin{aligned} U_i + K_i + W_{\text{friction/wrywing}} + W_{\text{applied/toegepas}} &= U_f + K_f \checkmark \\ 0 + f \Delta x \cos \theta + W_{\text{applied/toegepas}} &= mgh \quad (K_i = K_f) \\ 0 + (50)(10)(-1) \checkmark + W_{\text{applied/toegepas}} &= (120)(9,8)(1,5) \checkmark \checkmark \\ \therefore W_{\text{applied/toegepas}} &= 2\,264 \text{ J} \checkmark \quad (2,26 \times 10^3 \text{ J}) \end{aligned}$$

Accept/Aanvaar: E_k, E_p

Option 2/Opsie 2:

For equilibrium:/Vir ewewig:

$$F = f + W_{\text{parallel to incline/parallel met helling}} = f + mg \sin \alpha \quad (\alpha - \text{angle of incline with horizontal/hoek van helling met horisontaal})$$

$$F = 50 \checkmark + (120)(9,8)\left(\frac{1,5}{10}\right) \checkmark$$

$$\therefore F = 226,4 \text{ N}$$

$$\begin{aligned} W_{\text{applied/toegepas}} &= F \Delta x \cos \theta \checkmark \\ &= (226,4)(10)(\cos 0^\circ) \checkmark \text{ OR } (226,4)(10) \\ &= 2\,264 \text{ J} \checkmark \quad (2,26 \times 10^3 \text{ J}) \end{aligned}$$

Option 3/Opsie 3:

$$W_{\text{net/netto}} = \Delta K \checkmark$$

$$W_{\text{applied/toegepas}} + W_{\text{friction/wrywing}} + W_{\text{gravity/gravitasie}} = \Delta K$$

$$W_{\text{applied/toegepas}} + (50)(10)(-1) \checkmark - (120)(9,8)(1,5) \checkmark = 0 \checkmark$$

$$\therefore W_{\text{applied/toegepas}} = 2\,264 \text{ J} \checkmark \quad (2,26 \times 10^3 \text{ J})$$

Option 4/Opsie 4:

$$W_{\text{(external forces/eksterne kragte)}} = \Delta U + \Delta K \checkmark$$

OR/OF

$$W_{\text{applied/toegepas}} + W_{\text{friction/wrywing}} = (U_f - U_i) + (K_f - K_i) / \Delta U + \Delta K$$

$$W_{\text{applied/toegepas}} + (50)(10)(-1) \checkmark = (120)(9,8)(1,5) - 0 \checkmark + 0 \checkmark$$

$$\therefore W_{\text{applied/toegepas}} = 2\,264 \text{ J} \checkmark \quad (2,26 \times 10^3 \text{ J})$$

[12.1.3] (5)

5.3.2

$$\begin{aligned} W_{\text{applied/toegepas}} &= F \Delta x \cos \theta \checkmark \\ 2\,264 \text{ J} \checkmark &= F(10)(1) \checkmark \\ \therefore F &= 226,4 \text{ N} \checkmark \quad (2,26 \times 10^2 \text{ N}) \end{aligned}$$

OR/OF

$$F = f + W_{\text{par to incline/par met helling}} = f + mg \sin \beta \checkmark \quad (\alpha - \text{angle of incline with horizontal/hoek van helling met horisontaal})$$

$$F = 50 \checkmark + (120)(9,8)\left(\frac{1,5}{10}\right) \checkmark$$

$$\therefore F = 226,4 \text{ N} \checkmark \quad (2,26 \times 10^2 \text{ N})$$

[12.2.3] (4)

[12]

QUESTION 6/VRAAG 6

- 6.1 The net work done on an object is equal to the change in the object's kinetic energy. ✓✓

Only/Slegs $\frac{2}{2}$ or/of $\frac{0}{2}$

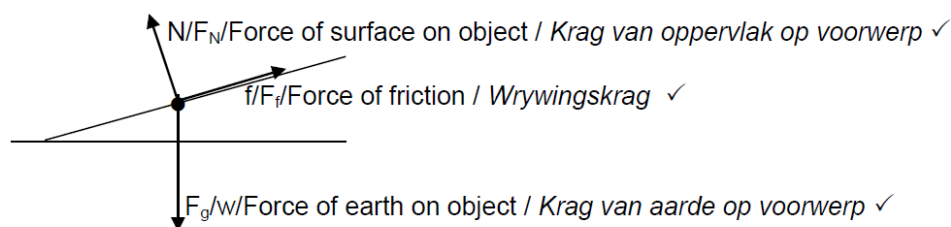
Die netto arbeid verrig op 'n voorwerp is gelyk aan die verandering in kinetiese energie van die voorwerp.

OR/OF

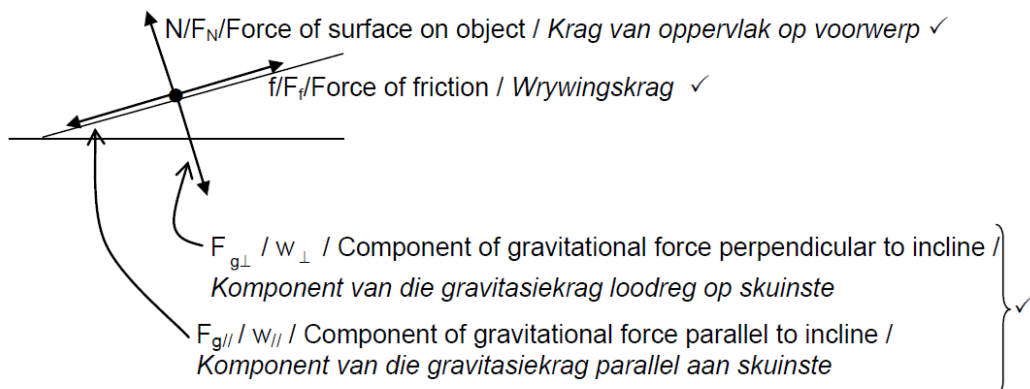
The work done on an object by a net force is equal to the change in the object's kinetic energy. / Die arbeid verrig op 'n voorwerp deur 'n netto krag is gelyk aan die verandering in kinetiese energie van die voorwerp.

[12.2.1] (2)

- 6.2



OR/OF



[12.1.2] (3)

6.3.1 $v_f^2 = v_i^2 + 2a\Delta x \checkmark$
 $= (0)^2 + (2)(2)(10) \checkmark$
 $= 40 \text{ m}^2 \cdot \text{s}^{-2} \checkmark$

+

$E_{kf} = \frac{1}{2}mv_f^2 \checkmark$
 $= \frac{1}{2}(60)(40) \checkmark$
 $= 1\,200 \text{ J} \checkmark$

OR/OF

$\Delta x = v_i \Delta t + \frac{1}{2}a\Delta t^2$

$10 = (0)\Delta t + \frac{1}{2}(2)\Delta t^2$

$\therefore \Delta t = 3,16 \text{ s}$

$v_f = v_i + a\Delta t = 0 + (2)(3,16) \checkmark = 6,32 \text{ m} \cdot \text{s}^{-1}$

$E_{kf} = \frac{1}{2}mv_f^2 \checkmark$
 $= \frac{1}{2}(60)(6,32)^2 \checkmark$
 $= 1\,200 \text{ J} \checkmark$

[12.1.3] (5)

6.3.2 $W_g = w_{\parallel} \Delta x \cos \theta \checkmark$
 $= mg \sin 25^\circ \checkmark (10)(\cos 0^\circ) \checkmark$
 $= (60)(9,8) \sin 25^\circ (1) \checkmark$
 $= 2\,485 \text{ J} \checkmark$

OR/OF

$W_g = w \Delta x \cos \theta \checkmark$
 $= mgh \cos 0^\circ$
 $= (60)(9,8) \checkmark (10) \sin 25^\circ (1) \checkmark$
 $= 2\,485 \text{ J} \checkmark$

OR/OF

$W_g = -\Delta U \checkmark$
 $= - (0 - mgh) \checkmark$
 $= - (0 - (60)(9,8)(10) \sin 25^\circ) \checkmark$
 $= 2\,485 \text{ J} \checkmark$

[12.2.3] (4)

Accept/Aanvaar:

E_k / K

$v^2 = u^2 + 2as / s = ut + \frac{1}{2}at^2 / v = u + at$

A mixture of the two allowed formulae is not accepted. / 'n Mengsel van die twee erkende formules word nie aanvaar nie.

6.3.3

OPTION 1/OPSIE 1:

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$W_{g(\text{parallel to slope/parallel aan helling})} + W_f = \Delta E_k \checkmark$$

$$2\,485 + W_f = 1\,200 \checkmark$$

$$W_f = -1\,285 \text{ J} \checkmark \text{ (If/Indien + 1 285 J deduct 1 mark/trek 1 punt af)}$$

Marking rule 1.6
Nasienreël 1.6

OPTION 2/OPSIE 2:

$$W_{\text{net}} = W_g + W_f \checkmark$$

$$ma\Delta x = W_g + W_f$$

$$(60)(2)(10) \checkmark = 2\,485 \checkmark + W_f$$

$$\therefore W_f = -1\,285 \text{ J} \checkmark \text{ (If/Indien + 1 285 J deduct 1 mark/trek 1 punt af)}$$

Marking rule 1.6
Nasienreël 1.6

OPTION 3/OPSIE 3:

$$W_{(\text{applied/toegepas})} = \Delta E_k + \Delta E_p - W_f$$

$$0 = (\frac{1}{2}mv_f^2 - 0) + (0 - mgh) - W_f \quad \text{Max./Maks.: } \frac{3}{4}$$

$$0 = \frac{1}{2}mv_f^2 - mgh - W_f \checkmark$$

$$0 = 1\,200 - 2\,485 - W_f \checkmark$$

$$\therefore W_f = -1\,285 \text{ J} \checkmark$$

$$W_{\text{appl/toegep}} = \Delta U + \Delta K + W_f \quad \frac{0}{4}$$

Marking rule 1.6
Nasienreël 1.6

OPTION 4 / OPSIE 4:

$$(U + K)_i + W_f = (U + K)_f \quad \text{Max./Maks.: } \frac{3}{4}$$

$$mgh + 0 + W_f = 0 + \frac{1}{2}mv_f^2 \checkmark$$

$$2\,485 + W_f = 1\,200 \checkmark$$

$$W_f = -1\,285 \text{ J} \checkmark \text{ (If/Indien + 1 285 J deduct 1 mark/trek 1 punt af)}$$

$$(U + K)_i - W_f = (U + K)_f \quad \frac{0}{4}$$

Marking rule 1.6
Nasienreël 1.6

OPTION 5/OPSIE 5:

$$W_{\text{nc}} = \Delta E_k + \Delta E_p \checkmark$$

$$= (\frac{1}{2}mv_f^2 - 0) + (0 - mgh)$$

$$= \frac{1}{2}mv_f^2 - mgh \checkmark$$

$$= 1\,200 - 2\,485 \checkmark$$

$$\therefore W_{\text{nc}} = W_f = -1\,285 \text{ J} \checkmark \quad \text{(If/Indien + 1 285 J deduct 1 mark/trek 1 punt af)}$$

Marking rule 1.6
Nasienreël 1.6

(4)

[12.2.3]

6.3.3

OPTION 1/OPSIE 1

$$W_f = F_f \Delta x \cos \theta \checkmark$$

$$- 1\,285 = f(10) \cos 180^\circ \checkmark$$

$$F_f = 128,5 \text{ N} \checkmark$$

OPTION 2/OPSIE 2

$$F_{\text{net}} = F_{g(\text{parallel to slope/parallel aan helling})} - F_f \checkmark$$

$$ma = mg \sin 25^\circ - F_f \checkmark$$

$$(60)(2) = (60)(9,8) \sin 25^\circ - F_f \checkmark$$

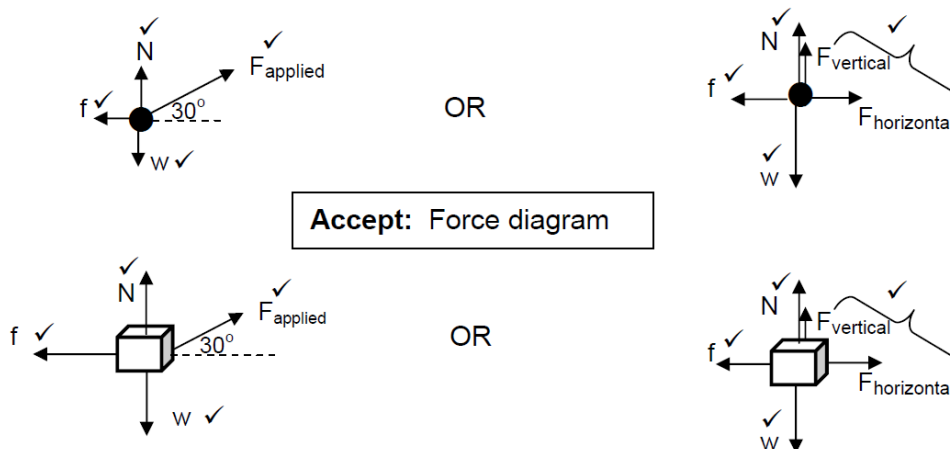
$$F_f = 128,5 \text{ N} \checkmark$$

[12.2.3] (3)
[21]

QUESTION 5

Accepted Labels	
N	Normal / Force of surface on crate / F_N / 269 N / 275 N
w	F_g / force of Earth on crate / weight / 294 N / 300 N mg / gravitational force
F_{applied}	F / force of worker on crate / 50 N / F_A
f	F_{friction} / 20 N / F_f / friction
$F_{\text{horizontal}}$ / F_x / $F_{\parallel}$	43,30 N
F_{vertical} / F_y / $F_{\perp}$	25 N

5.1



[12.1.2] (4)

5.2 $W = F \Delta x \cos 90^\circ \checkmark \checkmark = 0$

OR

They (normal force and the gravitational force) are perpendicular / at 90° to the (direction of the) displacement / motion / Δx $\checkmark \checkmark$ of the crate.

OR

The angle between the force and displacement / motion / Δx is 90° . $\checkmark \checkmark$

OR

The crate moves horizontally and the forces act vertically. $\checkmark \checkmark$

[12.2.2] (2)

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5.3

Accepted symbols for applied force: F_{appl} / F / F_A

Accepted symbols for frictional force: f / F_f / F_{friction}

Accepted symbols for gravitational force: w / F_g / $F_{\text{force of Earth on crate}}$ / gravitational force

OPTION 1

$$\begin{aligned} W_{\text{net}} &= W_{\text{appl}} + W_f \\ &= F_{\text{app}} \Delta x \cos \theta + f \Delta x \cos \theta \quad \left. \vphantom{\begin{aligned} W_{\text{net}} &= W_{\text{appl}} + W_f \\ &= F_{\text{app}} \Delta x \cos \theta + f \Delta x \cos \theta \end{aligned}} \right\} \checkmark \text{ For either formula} \\ &= (50)(6)(\cos 30^\circ) \checkmark + (20)(6)(\cos 180^\circ) \checkmark \\ &= 259,81 + (-120) \\ W_{\text{net}} &= 139,81 \text{ J } \checkmark \end{aligned}$$

OPTION 2

$$\begin{aligned} W_{\text{applied}} &= F_{\text{app}} \Delta x \cos \theta \\ &= (50)(6)(\cos 30^\circ) \checkmark \\ &= 259,81 \text{ J} \\ W_f &= f \Delta x \cos \theta \\ &= (20)(6)(\cos 180^\circ) \checkmark \\ &= -120 \text{ J} \end{aligned}$$

$$\begin{aligned} W_{\text{net}} &= W_{\text{applied}} + W_f \checkmark \text{ OR } F_{\text{app}} \Delta x \cos \theta + F \Delta x \cos \theta \\ &= 139,81 \text{ J } \checkmark \end{aligned}$$

OPTION 3

$$\begin{aligned} W_{\text{net}} &= W_{\text{appl} //} + W_f \quad \left. \vphantom{\begin{aligned} W_{\text{net}} &= W_{\text{appl} //} + W_f \\ &= F_{\text{app} //} \Delta x \cos \theta + f \Delta x \cos \theta \end{aligned}} \right\} \checkmark \text{ For either formula} \\ &= F_{\text{app} //} \Delta x \cos \theta + f \Delta x \cos \theta \\ &= (50)(\cos 30^\circ)(6) \cos 0^\circ \checkmark + (20)(6)(\cos 180^\circ) \checkmark \\ &= 259,81 + (-120) \\ W_{\text{net}} &= 139,81 \text{ J } \checkmark \end{aligned}$$

OPTION 4

$$\begin{aligned} F_{\text{net}} &= F_{\text{horizontal}} + f \\ &= (50)(\cos 30^\circ) + (-20) \checkmark \\ &= 23,30 \text{ N} \\ W_{\text{net}} &= F_{\text{net}} \Delta x \cos \theta \checkmark \\ &= (23,30)(6)(\cos 0^\circ) \checkmark \\ &= 139,81 \text{ J } \checkmark \end{aligned}$$

OPTION 5

$$\begin{aligned} F_{\text{net}} &= F_{\text{horizontal}} + f \\ ma &= (50)(\cos 30^\circ) + (-20) \checkmark \\ (30)a &= (50)(\cos 30^\circ) + (-20) \\ a &= 0,776 \dots \text{ m} \cdot \text{s}^{-2} \\ v_f^2 &= v_i^2 + 2a\Delta x \\ &= (0)^2 + 2(0,78 \dots)(6) \\ v_f &= 3,052 \dots \text{ m} \cdot \text{s}^{-1} \\ W_{\text{net}} &= \Delta K = \frac{1}{2} m(v_f^2 - v_i^2) \\ &= \frac{1}{2} (30)(3,052 \dots^2 - 0^2) \checkmark \\ &= 139,81 \text{ J } \checkmark \end{aligned}$$

✓ one mark for all three formulas

[12.1.3] (4)

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5.4

$$W_{\text{net}} = \Delta K / W_{\text{net}} = \Delta E_k \checkmark$$

$$= \frac{1}{2} mv_f^2 - \frac{1}{2} mv_i^2 \checkmark$$

$$\frac{139,81}{v_f} = \frac{1}{2} (30) v_f^2 - 0 \checkmark$$

$$v_f = 3,05 \text{ m}\cdot\text{s}^{-1} \checkmark$$

If: W instead of W_{net} max(2/3)

No marks for any other method

[12.2.3] (3)

5.5

Greater than ✓

The horizontal component (of the force) / force in direction of motion will now be greater / F_{net} will now be greater. ✓

OR

As θ decreases $\cos \theta$ increases ✓

OR

For θ smaller than 30° , $\cos \theta > \cos 30^\circ$. ✓

[12.3.2] (2)
[15]

QUESTION 5

- 5.1 R: Force of incline (surface) on crate / N / Normal (force) / F_N ✓
 S: Gravitational force / Gravity / force of Earth on crate /
 F_g / W / $F_{\text{Earth on crate}}$ ✓
 T: Frictional force / F_f / F_{friction} / f ✓

[12.1.2] (3)

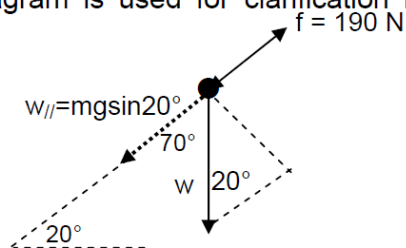
- 5.2 The force is perpendicular to ✓ the displacement ✓ of the crate.

OR

$$W = F \Delta x \cos 90^\circ \checkmark = 0 \checkmark$$

[12.2.1] (2)

- 5.3 The following diagram is used for clarification in the solutions below.



OPTION 1

$$\begin{aligned} W_{\text{net}} &= W_w + W_f \checkmark \\ &= mg \Delta x \cos 70^\circ + f \Delta x \cos 180^\circ \\ &= (70)(9,8) \checkmark (12)(\cos 70^\circ) \checkmark + (190)(12)(-1) \checkmark \\ W_{\text{net}} &= 535,51 \text{ J} \checkmark \end{aligned}$$

Accept:
 $\cos 180^\circ$ or -1

OPTION 2

$$\begin{aligned} F_{\text{net}} &= W_{\text{f}} + f \\ &= mg \sin 20^\circ + (-190) \\ &= (70)(9,8) \sin 20^\circ \checkmark - 190 \checkmark \\ &= 44,63 \text{ N} \end{aligned}$$

Accept:
 $\cos 0^\circ$ or 1

$$\begin{aligned} \therefore W_{\text{net}} &= F_{\text{net}} \Delta x \cos \theta \checkmark \\ &= (44,63)(12)(\cos 0^\circ) \checkmark \\ W_{\text{net}} &= 535,51 \checkmark \end{aligned}$$

OPTION 3

$$\begin{aligned} W_{\text{net}} &= W_{\text{w}} + W_{\text{f}} \checkmark \\ &= mg \sin 20^\circ \Delta x \cos 0^\circ + f \Delta x \cos 180^\circ \\ &= (70)(9,8) \sin 20^\circ \checkmark (12) \cos 0^\circ \checkmark + (190)(12) \cos 180^\circ \checkmark \\ W_{\text{net}} &= 535,51 \text{ J} \checkmark \end{aligned}$$

Accept:
 $\cos 0^\circ$ or 1
 $\cos 180^\circ$ or -1

OPTION 4

$$\begin{aligned} W_{\text{net}} &= W_{\text{w}} + W_{\text{f}} \checkmark \\ &= mgh \cos 0^\circ + f \Delta x \cos 180^\circ \\ &= (70)(9,8) \checkmark (12 \sin 20^\circ) \cos 0^\circ \checkmark + (190)(12) \cos 180^\circ \checkmark \\ W_{\text{net}} &= 535,51 \text{ J} \checkmark \end{aligned}$$

Accept:
 $\cos 0^\circ$ or 1
 $\cos 180^\circ$ or -1

5.3

[12.1.3] (5)

+

5.4

The net work done (on an object) $\checkmark$ is equal to the change in (the object's) kinetic energy. $\checkmark$

OR

The work done (on an object) by a net force is equal to the change in (the object's) kinetic energy.

[12.2.1] (2)

5.5

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \quad (\text{OR } W_{\text{net}} = \Delta E_k) \\ 535,51 &= \frac{1}{2} m (v_f^2 - v_i^2) \\ 535,51 \checkmark &= \frac{1}{2} (70) (v_f^2 - 4) \checkmark \\ v_f &= 4,39 \text{ m} \cdot \text{s}^{-1} \checkmark \end{aligned}$$

[12.2.3] (4)
[16]

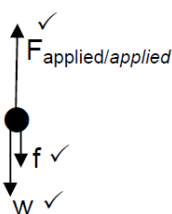
QUESTION 5 / VRAAG 5

- 5.1 The net (total) work (done on an object) ✓
 is equal to the change in kinetic energy (of the object.) ✓
Die netto (totale) arbeid (verrig op 'n voorwerp) ✓
is gelyk aan die verandering in kinetiese energie (van die voorwerp) ✓

OR / OF

The work done (on an object) by a net (resultant) force ✓
 is equal to the change in (the object's) kinetic energy. ✓
Die arbeid verrig (op 'n voorwerp) deur 'n netto (resulterende) krag ✓
is gelyk aan die verandering in kinetiese energie (van die voorwerp.) ✓ (2)

5.2



(3)

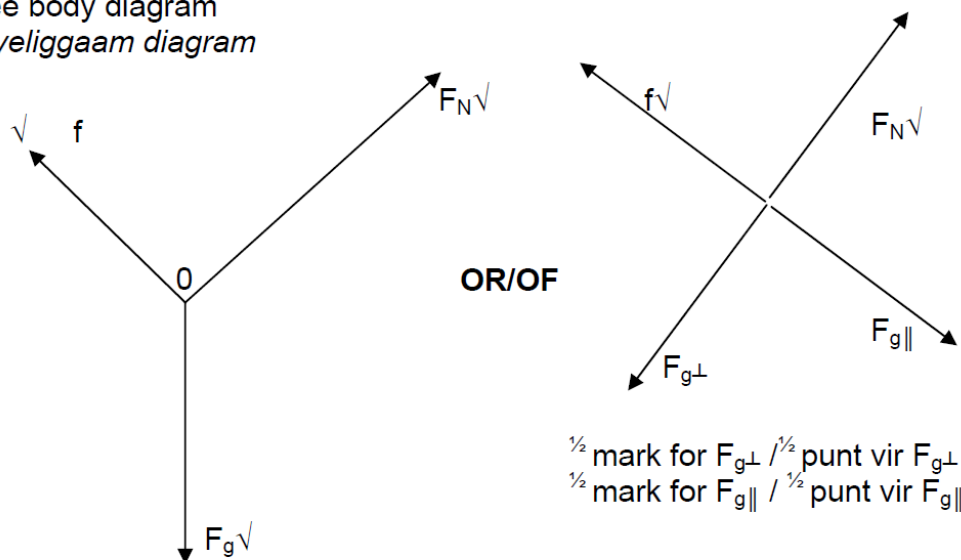
- 5.3 Gravitational force/weight (of soldier) ✓
Gravitasiekrag/gewig (van soldaat) (1)

- 5.4 $W_{\text{net}} = \Delta K$ ✓
 $F \Delta y \cos \theta + F_w \Delta y \cos \theta + W_f = \Delta K$
 $(960)(20) \cos 0^\circ \checkmark + (80)(9,8)(20) \cos 180^\circ \checkmark + W_f = 0 \checkmark$
 $19\,200 - 15\,680 + W_f = 0$
 $W_f = -3\,520 \text{ J}$ ✓

(5)
[11]

QUESTION/VRAAG 5

5.1 free body diagram
vryeliggaam diagram



F_N = Normal Force / normaalkrag

(3)

f = Frictional Force /wrywingkrag

F_g = Gravitational Force /gravitasiekrag

$F_{g\perp}$ = Component of gravitational force perpendicular to the slope
Komponent van gravitasiekrag loodreg op die skuinsvlak

$F_{g\parallel}$ = Component of Gravitational Force parallel to the slope
Komponent van gravitasiekrag parallel aan die skuinsvlak

(3)

$$\begin{aligned} 5.2 \quad 5.2.1 \quad F_{\text{Net}} &= F_{g\parallel} + f \\ &= mg \sin \alpha + f \\ &= (58)(9,8)(\sin 25^\circ) + 70 \\ &= 170,22 \text{ N downhill/afdraend} \end{aligned}$$

(3)

$$\begin{aligned} 5.2.2 \quad W_{\text{Net}} &= F_{\text{net}} \cos \theta \Delta x \\ &= (170,22 \cos 0^\circ) \times 57 \\ &= 9,69 \times 10^3 \text{ J} \end{aligned}$$

(3)

$$\begin{aligned} 5.2.3 \quad W_{\text{Net}} &= \Delta E_k \\ &= E_{kf} - E_{ki} \\ 9\,690 &= E_{kf} - \left(\frac{1}{2} 58 (3,6^2)\right) \\ E_{kf} &= 10\,065,84 \text{ J} \end{aligned}$$

(3)

$$\begin{aligned} 5.2.4 \quad E_{kf} &= \frac{1}{2} mv^2 \\ 10\,065,84 &= \frac{1}{2} 58 v_f^2 \\ v &= 18,63 \text{ m.s}^{-1} \end{aligned}$$

(3)

[15]

QUESTION 5/VRAAG 5

- 5.1 The energy of an object due to its position ✓
above the surface of the earth. ✓

*Die energie van 'n voorwerp as gevolg sy posisie ✓
bokant die oppervlak van die aarde. ✓*

(2)

5.2

Option 1/Opsie 1:

$$W_{\text{net}} = \Delta K \quad \checkmark$$

$$mg\Delta y \cos\theta + W_f = \frac{1}{2}m v_f^2 - \frac{1}{2}m v_i^2$$

$$(2)(9,8)(2)\cos 0^\circ \checkmark + W_f \checkmark = \frac{1}{2}(2)(5)^2 \checkmark - 0 \checkmark$$

$$\therefore W_f = -14,2 \text{ J} \quad \checkmark$$

Option 2/Opsie 2:

$$W_{\text{net}} = \Delta K \quad \checkmark$$

$$-\Delta U + W_f = \frac{1}{2}m v_f^2 - \frac{1}{2}m v_i^2$$

$$mgh + W_f = \frac{1}{2}m v_f^2 - \frac{1}{2}m v_i^2$$

$$(2)(9,8)(2) \checkmark + W_f \checkmark = \frac{1}{2}(2)(5)^2 \checkmark - 0 \checkmark$$

$$\therefore W_f = -14,2 \text{ J} \quad \checkmark$$

(6)

- 5.3 No/Nee ✓

Friction is present/Wrywing is aanwesig. ✓

(2)

- 5.4.1 $\Sigma p_{\text{before}} = \Sigma p_{\text{after}} \quad \checkmark$

$$(2)(5) + (9)(0) \checkmark = 2v_{f2} + (9)(1) \checkmark$$

$$\therefore v_{f2} = 0,5 \text{ m}\cdot\text{s}^{-1} \quad \checkmark$$

Notes/Aantekeninge:

Other formulae/Ander formules:

$$m_1 v_{i1} + m_2 v_{i2} = m_1 v_{f1} + m_2 v_{f2}$$

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

(4)

- 5.4.2 $K(\text{total after/total na}) = \frac{1}{2}m_1 v_f^2 + \frac{1}{2}m_2 v_f^2 \quad \checkmark$

$$= \frac{1}{2}(2)(0,5)^2 \checkmark + \frac{1}{2}(9)(1)^2 \checkmark$$

$$= 4,75 \text{ J} \quad \checkmark$$

$$K(\text{total before}) \neq K(\text{total after}) \quad \checkmark$$

$\therefore$ inelastic

$$K(\text{totaal na}) \neq K(\text{totaal voor}) \quad \checkmark$$

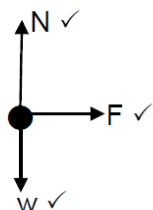
$\therefore$ onelasties

(5)

[19]

QUESTION 5/VRAAG 5

5.1



(3)

- 5.2 The net (total) work (done on an object) is equal to ✓
the change in kinetic energy (of the object.) ✓
Die netto (totale) arbeid verrig (op 'n voorwerp) is gelyk aan ✓
die verandering in kinetiese energie (van die voorwerp). ✓

(2)

5.3

- 5.3.1 $W_{\text{net}} = \Delta E_k / \Delta K$ ✓ **OR/OF** $F_{\text{net}} \Delta x \cos \theta = \frac{1}{2} m (v_f^2 - v_i^2)$
 $F_{\text{net}} (1,02) \cos 180^\circ \checkmark = \frac{1}{2} (1\,200) (0 - 20^2)$ ✓
 $F_{\text{net}} = 235\,294,12 \text{ N}$ ✓ ($2,35 \times 10^5 \text{ N}$)

(4)

5.3.2

<u>OPTION 1 / OPSIE 1</u>	<u>OPTION 2 / OPSIE 1</u>
$F_{\text{net}} \Delta t = m \Delta v$ ✓	$\Delta x = \left(\frac{v_i + v_f}{2} \right) \Delta t$ ✓
$\therefore (-235\,294,12) \Delta t \checkmark = (1\,200) (0 - 20)$ ✓	$1,02 \checkmark = \left(\frac{20 + 0}{2} \right) \Delta t$ ✓
$\therefore \Delta t = 0,1 \text{ s}$ ✓ (0,102 s)	$\Delta t = 0,1 \text{ s}$ ✓

(4)

[13]

QUESTION 5/VRAAG 5

- 5.1 The total mechanical energy remains constant / is conserved ✓
in a closed / isolated system / in absence of external forces /non-conservative forces. ✓

*Die totale meganiese energie in bly konstant / bly behoue
in 'n geslote / geïsoleerde sisteem /in afwesigheid van eksterne kragte /nie-
konserwatiewe kragte.*

OR/OF

The sum of the potential and kinetic energy of a system remains constant ✓
in a closed/isolated system. ✓

*Die som van die potensiële en kinetiese energie van 'n sisteem bly konstant
in 'n geslote / geïsoleerde sisteem.*

OR/OF

When the work done on an object by the non-conservative forces is zero ✓,
the total mechanical energy is conserved. ✓

*Wanneer die arbeid deur die nie-konserwatiewe kragte op 'n voorwerp verrig
nul is, bly die totale meganiese energie behoue.*

(2)

5.2

OPTION 1/OPSIE 1

$$\left. \begin{aligned} E_{\text{mechanical at X}} &= E_{\text{mechanical at Y}} \\ (E_p + E_k)_X &= (E_p + E_k)_Y \\ (mgh + \frac{1}{2}mv^2)_X &= (mgh + \frac{1}{2}mv^2)_Y \\ \underline{5(9,8)(5) + \frac{1}{2}(5)(0^2)} &= \underline{5(9,8)(1) + \frac{1}{2}(5)v_f^2} \\ v &= 8,85 \text{ m}\cdot\text{s}^{-1} \end{aligned} \right\} \checkmark \text{ Any one/Enige een}$$

OPTION 2/OPSIE 2

$$\left. \begin{aligned} E_{\text{mechanical at X}} &= E_{\text{mechanical at Y}} \\ (E_p + E_k)_X &= (E_p + E_k)_Y \\ (mgh + \frac{1}{2}mv^2)_X &= (mgh + \frac{1}{2}mv^2)_Y \\ \underline{5(9,8)(4) + \frac{1}{2}(5)(0^2)} &= \underline{5(9,8)(0) + \frac{1}{2}(5)v_f^2} \\ v &= 8,85 \text{ m}\cdot\text{s}^{-1} \end{aligned} \right\} \checkmark \text{ Any one/Enige een}$$

(4)

5.3

Weight / gravitational (force) / (force of) gravity ✓

Gewig / Gravitatie(krag)

Normal force / Normaalkrag ✓

(2)

5.4

Z to/na Y ✓

(1)

5.5

OPTION 1/OPSIE 1

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \\ W_w + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ mg\Delta y \cos 0^\circ + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ \underline{5(9,8)(1)(1) \checkmark + (10)\Delta x(-1) \checkmark} &= \underline{\frac{1}{2}(5)(4^2 - 8,85^2) \checkmark} \\ \Delta x &= 20,48 \text{ m} \checkmark \end{aligned}$$

OPTION 2/OPSIE 2

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \\ W_w + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ -\Delta E_p + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ -(0 - mgh) + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ \underline{5(9,8)(1) \checkmark + (10)\Delta x(-1) \checkmark} &= \underline{\frac{1}{2}(5)(4^2 - 8,85^2) \checkmark} \\ \Delta x &= 20,48 \text{ m} \checkmark \end{aligned}$$

OPTION 3/OPSIE 3

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \\ W_w + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ -\Delta E_p + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ -(0 - mgh) + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ \underline{5(9,8)(5) \checkmark + (10)\Delta x(-1) \checkmark} &= \underline{\frac{1}{2}(5)(4^2 - 0^2) \checkmark} \\ \Delta x &= 20,48 \text{ m} \checkmark \end{aligned}$$

OPTION 4/OPSIE 4

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \\ W_w + W_f &= \frac{1}{2}m(v_f^2 - v_i^2) \\ mg\Delta x \cos(90^\circ - \theta) + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ mg\Delta x \sin \theta + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ mg\Delta x \left(\frac{1}{\Delta x} \right) + f\Delta x \cos 180^\circ &= \frac{1}{2}m(v_f^2 - v_i^2) \\ \underline{5(9,8) \checkmark + (10)\Delta x(-1) \checkmark} &= \underline{\frac{1}{2}(5)(4^2 - 8,85^2) \checkmark} \\ \Delta x &= 20,48 \text{ m} \checkmark \end{aligned}$$

OPTION 5/OPSIE 5

$$W_{\text{net}} = \Delta K \checkmark$$

$$W_{\text{w||}} + W_f = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$mg\sin\theta\Delta x\cos\theta + f\Delta x\cos\theta = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$mg\left(\frac{1}{\Delta x}\right)\Delta x\cos 0^\circ + f\Delta x\cos 180^\circ = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$(5)(9,8) \checkmark + (10)\Delta x(-1) \checkmark = \frac{1}{2}(5)(4^2 - 8,85^2) \checkmark$$

$$\Delta x = 20,48 \text{ m} \checkmark$$

OPTION 6/OPSIE 6

$$W_{\text{net}} = \Delta K \checkmark$$

$$F_{\text{net}}\Delta x\cos\theta = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$(10 - 49\sin\theta)\Delta x\cos 180^\circ = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$(10 - 49\left(\frac{1}{\Delta x}\right))\Delta x\cos 180^\circ = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$(10\Delta x - 49)(-1)\checkmark = \frac{1}{2}(5)(4^2 - 8,85^2) \checkmark$$

$$\Delta x = 20,48 \text{ m}$$

OPTION 7/OPSIE 7

$$W_{\text{nc}} = \Delta E_p + \Delta E_k \checkmark$$

$$f\Delta x\cos\theta = (mgh_f - mgh_i) + \left(\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2\right)$$

$$(10)\Delta x\cos 180^\circ \checkmark = [0 - (5)(9,8)(1)] \checkmark + \left[\frac{1}{2}(5)(4)^2 - \frac{1}{2}(5)(8,85)^2\right] \checkmark$$

$$\Delta x = 20,48 \text{ m} \checkmark$$

(5)

5.6 Equal to / Gelyk aan $\checkmark$

(1)

[15]

QUESTION/VRAAG 4

- 4.1 Its velocity decreases $\checkmark$ (from 12 m.s^{-1} to 0 m.s^{-1}) as it moves up $\checkmark$ /uniform deceleration as it moves up.
Sy snelheid neem af $\checkmark$ (van 12 m.s^{-1} tot 0 m.s^{-1}) terwyl dit op beweeg $\checkmark$ /uniforme vertraging terwyl dit op beweeg. [12.2.1] (2)

4.2 $\Delta E_k = E_{kf} - E_{ki} \checkmark$
 $= \frac{1}{2} (5)(0)^2 - \frac{1}{2} (5)(12)^2 \checkmark$
 $= -360 \text{ J} \checkmark$ [12.1.3] (3)

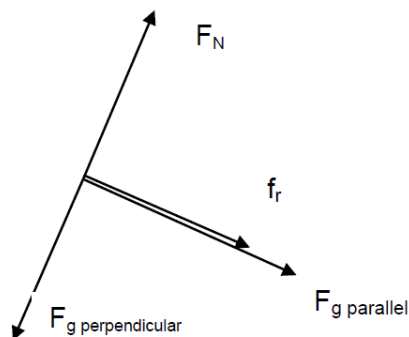
- 4.3 POSITIVE MARKING FROM 4.2/POSITIEWE NASIEN VAN 4.2
 $-360 \text{ J} \checkmark$ [12.1.3] (1)

- 4.4 The work done by a net force (on an object) is equal to $\checkmark$ the change in kinetic energy (of that particular object). $\checkmark$
Die arbeid verrig deur 'n netto/resultante krag is gelyk aan $\checkmark$ die verandering in kinetiese energie (van die voorwerp). $\checkmark$

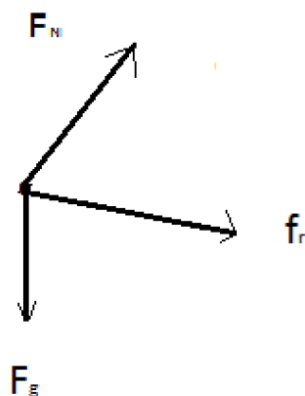
OR/OF

The net/total work (done on an object) is equal to $\checkmark$ the change in kinetic energy (of the object). $\checkmark$
Die netto/totale arbeid verrig (op 'n voorwerp) is gelyk aan $\checkmark$ die verandering in kinetiese energie (van die voorwerp). $\checkmark$ [12.12.1] (2)

4.5



4.5



One mark for $F_N \rightarrow$ Normal force/
normaalkrag
One mark for $F_{fr} \rightarrow$ frictional
force/wrywing
One mark for $F_{g\perp}$ and $F_{g\parallel}$
(components of gravitational force)
/komponente van gravitasiekras

OR/OF

one mark for F_g gravitational force/
gravitasiekras

[12.1.3] (3)

4.6

$$\begin{aligned} W_{Fg} &= F_g \cos \Theta \Delta x \checkmark \\ &= mg \cos \Theta \Delta x \\ &= 5 \times 9,8 \cos (16^\circ + 90^\circ)(8,4) \checkmark \\ &= -113,45 \text{ J } \checkmark \end{aligned}$$

OR/OF

$$\begin{aligned} W_{Fg} &= mg \Delta h \checkmark \\ &= 5 (9,8) (0-8,4 \sin 16^\circ) \checkmark \\ &= -113,45 \text{ J } \checkmark \end{aligned}$$

[12.1.3] (3)

4.7

POSITIVE MARKING FROM/POSITIEWE NASIEN VAN
QUESTION/VRAAG 4.2 AND/EN QUESTION/VRAAG 4.6

$$\begin{aligned} W_{NET} &= \Delta E_k \checkmark \\ W_{fr} + W_{Fg\parallel} \checkmark &= \Delta E_k \quad (W_N = 0 \text{ J and/en } W_{Fg\perp} = 0 \text{ J}) \text{ since/omdat } \cos 90^\circ = 0 \\ W_{fr} + (-113,45) \checkmark &= -360 \checkmark \\ W_{fr} &= -246,55 \text{ J } \checkmark \end{aligned}$$

OR/OF

$$\begin{aligned} W_{NET} &= \Delta E_k \checkmark \\ F_{NET} \Delta x \cos \Theta \checkmark &= \Delta E_k \\ F_{NET} (8,4) \cos 180^\circ &= -360 \checkmark \\ (F_{fr} + F_{g\parallel}) (8,4) \cos 180^\circ &= -360 \\ F_{fr} (8,4) \cos 180^\circ + f_{g\parallel} (8,4) \cos 180^\circ &= -360 \\ W_{fr} + 13,506 (-1) 8,4 \checkmark &= -360 \\ W_{fr} &= -246,55 \text{ J } \checkmark \end{aligned}$$

[12.1.3] (5)
[19]

QUESTION 4/VRAAG 4

4.1	$W_{\text{net}} = \Delta K$ ✓ $W_{\text{net}} = \frac{1}{2} (M + m)(v_f^2 - v_i^2)$ ✓ $W_{\text{fr}} = f\Delta x \cos\theta$ ✓ = $\frac{1}{2} (M + m)(v_f^2 - v_i^2)$ $\frac{10 \times 2 \cos 180^\circ}{v_{\text{bb}}} = \frac{1}{2} (7,02)(0 - v^2)$ ✓ $v_{\text{bb}} = 2,39 \text{ m}\cdot\text{s}^{-1}$ ✓ (2,387) $\text{m}\cdot\text{s}^{-1}$	Notes / Aantekeninge 1 mark for either of the formulae indicated 1 punt vir enige van die formules aangedui Accept/Aanvaar $W_{\text{nc}} = \Delta K + \Delta U$ with $\Delta U = 0$	(5)
-----	--	--	-----

4.2	<u>The total linear momentum of an (isolated) closed system remains constant.</u> <u>Die totale lineêre momentum in 'n geslote (geïsoleerde) sisteem bly konstant</u> ACCEPT/AANVAAR <u>In an isolated system the total momentum before collision equals the total momentum after collision.</u> <u>In 'n (geïsoleerde) geslote sisteem is die totale momentum voor botsing gelyk aan die totale momentum na botsing.</u>	Notes/Aantekeninge 2 or/of 0	(2)
-----	--	--	-----

4.3.	Positive marking from QUESTION 4.1 Positiewe nasien vanaf VRAAG 4.1 $\Sigma p_i = \Sigma p_f$ ✓ $m_1 v_{1i} + m_2 v_{2i} = (m_1 + m_2) v_f$ $0,02 v_i + (7)(0) = (7,02)(2,39)$ $0,02 v_i = 7,02 (2,39)$ ✓ $v_i = 838,89 \text{ m}\cdot\text{s}^{-1}$ ✓	Notes / Aantekeninge Accept/Aanvaar $(m_1 + m_2) v_i = m_1 v_{1f} + m_2 v_{2f}$ $837,84 \text{ m}\cdot\text{s}^{-1}$ (for learners working with $2,387 \text{ m}\cdot\text{s}^{-1}$ / vir leerders wat met $2,387 \text{ m}\cdot\text{s}^{-1}$ werk)	(4) [11]
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QUESTION 5/VRAAG 5

- 5.1 If the work done in moving an object between two points depends on the path taken (then the force applied is non-conservative) ✓✓ (2 or/of 0).

Indien die arbeid verrig om 'n voorwerp tussen twee punte te beweeg, afhanklik is van die pad wat gevolg word, (is die krag wat toegepas word, nie-konserwatief)

(2)

- 5.2.1 No/Nee ✓

(1)

- 5.2.2 Since there is no acceleration, the net force is zero ✓ hence net work done (which is $F_{\text{net}} \Delta x \cos \theta$) must be zero. ✓

Omdat daar geen versnelling is nie, is die netto krag nul. Dus moet die netto arbeid verrig (wat $F_{\text{net}} \Delta x \cos \theta$ is) nul wees.

OR/OF

$$W_{\text{net}} = \Delta K.$$

Since it is moving with constant velocity ✓ *Omdat dit teen konstante snelheid beweeg*

$$\Delta K = 0 \therefore W_{\text{net}} = 0 \checkmark$$

(2)

- 5.3

$$F_{\parallel} - (f + F) = 0 \checkmark$$

OR/OF

$$F = mg \sin \theta - f_k$$

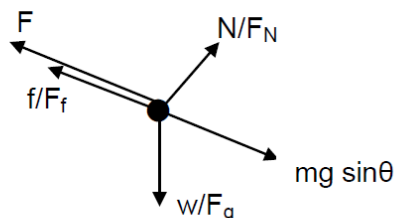
OR/OF

$$F = m g \sin \theta - 266$$

$$F = [100(9,8) \sin 25^\circ] \checkmark - 266 \checkmark$$

$$414,167 - 266$$

$$F = 148,17 \text{ N} \checkmark$$



(4)

NOTE/LET WEL

No mark for diagram / Geen punt vir diagram nie

1 mark for use of any of the three formulae / 1 punt vir gebruik van enige drie van die formules

5.4

OPTION 1/OPSIE 1

$$W = F \Delta x \cos \theta$$

$$W_{\text{net}} = W_f + W_g + W_N$$

$$W_{\text{net}} = f_k \Delta x \cos 180^\circ \checkmark + mg \sin \theta \Delta x \cos 0^\circ + 0$$

$$= (266)(3)(-1) \checkmark + [100(9,8) \sin 25^\circ (3)(1)] \checkmark + 0$$

$$= 444,5 \text{ J}$$

$$W_{\text{net}} = \Delta E_K / \Delta K = \frac{1}{2} m(v_f^2 - v_i^2) \checkmark$$

$$444,5 = \frac{1}{2} (100) (v_f^2 - 0) \checkmark$$

$$v_f = 2,98 \text{ m} \cdot \text{s}^{-1} \checkmark$$

1 mark for any of the three/
1 punt vir enige van die drie

(6)

OPTION 2/OPSIE 2

$$W_{\text{nc}} = \Delta E_p + \Delta E_k \checkmark$$

$$f \Delta x \cos \theta \checkmark = (mgh_f - mgh_i) + (\frac{1}{2} mv_f^2 - \frac{1}{2} mv_i^2)$$

$$266 \Delta x \cos 180^\circ \checkmark = (0 - mg \sin 25^\circ \Delta x \cos 0^\circ) + (\frac{1}{2} mv_f^2 - 0)$$

$$266(3)(-1) = [-100(9,8) \sin 25^\circ (3)(1)] \checkmark - \frac{1}{2} (100) (v_f^2 - 0) \checkmark$$

$$v_f = 2,98 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

OPTION 3/OPSIE 3

POSITIVE MARKING FROM QUESTION 5.3

POSITIEWE NASIEN VANAF VRAAG 5.3

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$F_{\text{net}} \Delta x \cos \theta \checkmark = \frac{1}{2} m(v_f^2 - v_i^2)$$

$$(148,17) \checkmark (3) \cos 0^\circ \checkmark = \frac{1}{2} (100) (v_f^2 - 0^2)$$

$$444,51 = 50 v_f^2 \checkmark$$

$$v_f = 2,98 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

OPTION 4/OPSIE 4

POSITIVE MARKING FROM QUESTION 5.3

POSITIEWE NASIEN VANAF VRAAG 5.3

$$F_{\text{net}} = ma \checkmark$$

$$148,17 \checkmark = 100a \checkmark$$

$$a = 1,48 \text{ m} \cdot \text{s}^{-2} \checkmark$$

$$v_f^2 = v_i^2 + 2a \Delta x \checkmark$$

$$= 2(1,48)(3) \checkmark$$

$$v_f = 2,98 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

OPTION 5/OPSIE 5

POSITIVE MARKING FROM QUESTION 5.3

POSITIEWE NASIEN VANAF VRAAG 5.3

$$F_{\text{net}} = ma \checkmark$$

$$148,17 \checkmark = 100a \checkmark$$

$$a = 1,48 \text{ m} \cdot \text{s}^{-2}$$

$$\Delta x = v_i \Delta t + \frac{1}{2} a \Delta t^2$$

$$3 = 0 + \frac{1}{2} (1,48) \Delta t^2$$

$$\Delta t = 2,01 \text{ s}$$

$$v_f = v_i + a \Delta t$$

$$= 0 + (1,48)(2,01) \checkmark$$

$$v_f = 2,97 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

OPTION 6/OPSIE 6

POSITIVE MARKING FROM QUESTION 5.3

POSITIEWE NASIEN VANAF VRAAG 5.3

$$F_{\text{net}} = ma \checkmark$$

$$148,17 \checkmark = 100a \checkmark$$

$$a = 1,48 \text{ m} \cdot \text{s}^{-2}$$

$$\Delta x = v_i \Delta t + \frac{1}{2} a \Delta t^2$$

$$3 = 0 + \frac{1}{2} (1,48) \Delta t^2$$

$$\Delta t = 2,01 \text{ s}$$

$$\Delta y = \left(\frac{v_i + v_f}{2} \right) \Delta t$$

$$3 = \left(\frac{0 + v_f}{2} \right) (2,01)$$

$$v_f = 2,99 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

[15]

QUESTION 4/VRAAG 4

- 4.1 TO THE LEFT/NA LINKS ✓ ? (1)
- 4.2 (Newton's) Third Law (of motion)/(Newton) se Derde (Bewegingswet). ✓ (1)
- 4.3 In an isolated/closed system, ✓ the total mechanical energy is conserve remains constant. ✓
In 'n geïsoleerde/geslote sisteem ✓ bly die totale meganiese energie behoue/bly konstant. ✓

OR/OF

The total mechanical energy of a system remain constant ✓ provided the net work done by external non conservative forces is zero. ✓
Die totale meganiese energie van 'n sisteem bly konstant, ✓ mits die arbeid verrig deur eksterne nie-konservatiewe kragte, nul is. ✓

OR/OF

In the absence of a non-conservative force, ✓ the total mechanical energy is conserved/remains constant. ✓

In die afwesigheid van 'n nie-konservatiewe krag, ✓ bly die totale meganiese energie behoue/konstant. ✓

OR/OF

In an isolated/closed system, ✓ the sum of kinetic and gravitational potential energy is conserved/remains constant. ✓

In 'n geïsoleerde/geslote sisteem, ✓ bly die som van kinetiese en gravitasionele potensiele energie behoue/bly konstant. ✓

Notes/Aantekeninge:

Allocate ONE mark for 'isolated system' only in conjunction with energy.

Ken EEN punt toe vir "geïsoleerde/geslote sisteem" slegs indien saam met energie gebruik. 1/2

(2)

4.4

OPTION 1/OPSIE 1 $E_{\text{mechanical at A}} = E_{\text{mechanical at B}}$ $(E_p + E_k)_A = (E_p + E_k)_B$ $(mgh + \frac{1}{2}mv^2)_A = (mgh + \frac{1}{2}mv^2)_B$ $66(9,8)(0) + \frac{1}{2}(66)v^2 = 66(9,8)(1,6) + \frac{1}{2}(66)(0)^2$ $v = 5,6 \text{ m.s}^{-1}$ ✓		} ✓ Any ONE/Enige EEN (4)
OPTION 2/OPTION 2 $E_{\text{mechanical at A}} = E_{\text{mechanical at B}}$ $(E_p + E_k)_A = (E_p + E_k)_B$ $(mgh + \frac{1}{2}mv^2)_A = (mgh + \frac{1}{2}mv^2)_B$ $v^2 = 2gh$ $= (2)(9,8)(1,6)$ $v = 5,6 \text{ m.s}^{-1}$ ✓		} ✓ Any ONE/Enige EEN (4)
OPTION 3/OPSIE 3 $W_{\text{net}} = \Delta E_k$ $F_{\text{net}} \Delta y \cos \theta = \frac{1}{2}m(v_f^2 - v_i^2)$ $m(9,8)(1,6) \cos 0^\circ = \frac{1}{2}m(v_f^2 - 0^2)$ $v_f = 5,6 \text{ m.s}^{-1}$ ✓		} ✓ Any ONE/Enige EEN (4)
NOTES/AANTEKENINGE: Accept/Aanvaar $(E_p + E_k)_{\text{top}} = (E_p + E_k)_{\text{bottom}}$ $(U + K)_A = (U + K)_B$ $(U + K)_{\text{top}} = (U + K)_{\text{bottom}}$ $\Delta E_p + \Delta E_k = 0 / \Delta U + \Delta K = 0$		(4)

4.5 POSITIVE MARKING FROM QUESTION 4.4 POSITIEWE NASIEN VAN VRAAG 4.4

OPTION1/OPSIE1

$$\begin{aligned} \sum p_i &= \sum p_f \\ (m_B + m_P)v_{BPi} &= m_B v_{fi} + m_P v_{Pf} \quad \checkmark \text{ Any ONE/Enige EEN} \\ (70)(5) \checkmark &= (66)(5,6) + 4v_{Pf} \checkmark \\ v_{Pf} &= -4,9 \text{ m.s}^{-1} \\ &= 4,9 \text{ m.s}^{-1} \text{ to the left/na links } \checkmark \end{aligned} \quad (4)$$

OPTION2/OPSIE2

$$\begin{aligned} \Delta p_{\text{Boy}} &= -\Delta p_{\text{parcel}} \checkmark \\ m_{\text{boy}}(v_f - v_i) &= -m_p(v_f - v_i) \\ (66)(5,6 - 5) \checkmark &= -4(v_{Pf} - 5) \checkmark \\ v_{Pf} &= -4,9 \text{ m.s}^{-1} \\ &= 4,9 \text{ m.s}^{-1} \text{ to the left/Na links } \checkmark \end{aligned} \quad (4)$$

OPTION 3/OPSIE3

$$\begin{aligned} F_{BP} &= -F_{PB} \checkmark \\ m_B a_B &= -m_P a_P \\ m_B \left[\frac{v_{Bf} - v_{Bi}}{\Delta t} \right] &= -m_P \left[\frac{v_{Pf} - v_{Pi}}{\Delta t} \right] \\ \frac{(66)(5,6 - 5)}{\Delta t} \checkmark &= \frac{-4(v_{Pf} - 4,5)}{\Delta t} \checkmark \\ v_{Pf} &= -4,9 \text{ m.s}^{-1} \\ &= 4,9 \text{ m.s}^{-1} \text{ to the left/na links } \checkmark \end{aligned} \quad (4)$$

Other formulae/Ander formules:

$$\begin{aligned} m_1 v_{i1} + m_2 v_{i2} &= m_1 v_{f1} + m_2 v_{f2} \\ (m_1 + m_2) v &= m_1 v_{f1} + m_2 v_{f2} \\ m_1 v_{iB} + m_2 v_{iP} &= m_1 v_{fB} + m_2 v_{fP} \\ m_1 u_1 + m_2 u_2 &= m_1 v_1 + m_2 v_2 \\ p_{\text{total before}} &= p_{\text{total after}} \end{aligned}$$

Accept/Aanvaar:

$$p_{\text{before}} = p_{\text{after}} \quad \text{or/of} \quad p_i = p_f \quad (4)$$

4.6 INCREASES/VERHOOG $\checkmark$

$\ominus$ Δp parcel increases, thus Δp boy increases. $\checkmark$
For the same mass of boy, v will be greater. $\checkmark$

Δp pakkie vermeerder, dus Δp seun vermeerder. $\checkmark$
Vir dieselfde massa, van die seun sal v groter wees. $\checkmark$

OR/OF

If v of parcel increases, the momentum of the boy increases. $\checkmark$
For the same mass of boy, the velocity of parcel increases. $\checkmark$

Indien v van die pakkie toeneem, neem die momentum van die seun toe. $\checkmark$
Vir dieselfde massa van die seun, vermeerder die snelheid van die pakkie. $\checkmark$

OR/OF

F on parcel increases, therefore F on boy increases. ✓
 $F\Delta t$ (boy) increases, for the same mass of boy, thus v will increase. ✓

F op pakkie neem toe, dus neem F op seun toe. ✓
 $F\Delta t$ (seun) neem toe, dus vir dieselfde massa van seun sal V verhoog. ✓

OR/OF

$$-m_B v_{Bf} = m_P v_{Pf}$$

$$\text{AFR: } -m_S v_{Sf} = m_P v_{Pf}$$

$$v_B = -\frac{m_P v_{Pf}}{m_B} \quad \checkmark \text{ for same } m_B, \text{ if } v_P \text{ increases, } \checkmark \text{ then } v_B \text{ increases.}$$

$$v_S = -\frac{m_P v_{Pf}}{m_S} \quad \checkmark \text{ vir dieselfde } m_S, \text{ as } v_P \text{ toeneem, } \checkmark \text{ neem } v_S \text{ toe}$$

(3)
[15]

QUESTION 5/VRAAG 5

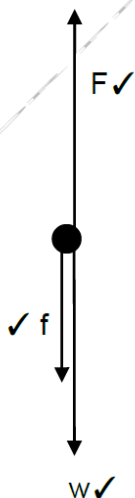
- 5.1 The net/total work done ✓ is equal to the change in the object's kinetic energy. ✓
Die netto/totale arbeid verrig ✓ op 'n voorwerp is gelyk aan die verandering in kinetiese energie van die voorwerp. ✓

OR/OF

The work done on an object by a resultant/net force ✓ is equal to the change in the object's kinetic energy. ✓
Die arbeid verrig op die voorwerp deur 'n resulterende/netto krag ✓ is gelyk aan die verandering in kinetiese energie van die voorwerp. ✓

(2)

5.2



Accepted labels/Aanvaarde benoemings	
W	$F_g/F_w/mg$ /gravitational force/weight F_g/F_w /gravitasiekrag/gewig
F	$F_{\text{applied}}/F_{\text{cable}}$ /Tension/T/17 000 N $F_{\text{toegepas}}/F_{\text{kabel}}$ /Spanning/T/17 000 N
f	F_f/F_{friction} /friction/air resistance F_f/F_{wrywing} /wrywing/lugweerstand

(3)

5.3

OPTION 1/OPSIE 1

$$W_{\text{net}} = \Delta E_k$$

$$W_T + W_W + W_f = \Delta E_k$$

$$F_T \Delta y \cos \theta + F_g \Delta y \cos \theta + W_f = 0$$

$$(17000)(20) \cos 0^\circ + (1680)(9,8)(20) \cos 180^\circ + W_f = 0$$

$$W_f = -10720 \text{ J}$$

✓ Any ONE/Enige EEN

(5)

OPTION 2/OPSIE 2

Downwards as positive

$$F_{\text{net}} = ma$$

$$-F + f + W = ma$$

$$-17000 + f + (1680)(9,8) = 0$$

$$f = 536 \text{ N}$$

$$W_f = f \Delta y \cos \theta$$

$$= (536)(20) \cos 180^\circ$$

$$= (536)(20)(-1)$$

$$= -10720 \text{ J}$$

(5)

Upwards as positive

$$F_{\text{net}} = ma$$

$$F + f + W = ma$$

$$17000 - f - (1680)(9,8) = 0$$

$$f = 536 \text{ N}$$

$$W_f = f \Delta y \cos \theta$$

$$= (536)(20) \cos 180^\circ$$

$$= (536)(20)(-1)$$

$$= -10720 \text{ J}$$

(5)

[10]

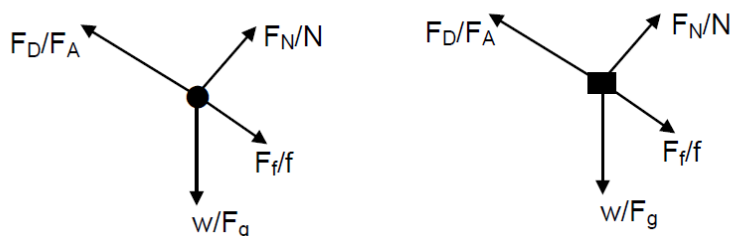
QUESTION 5/VRAAG 5

5.1

OPTION 1/OPSIE 1 $v_{ave} = \frac{800}{75} \checkmark = 10,67 \text{ m} \cdot \text{s}^{-1}$ $P_{ave} = Fv_{ave} \checkmark$ $P_{ave} = 240 (10,67)$ $= 2\,560,8 \text{ W (2,56 kW)} \checkmark$	OPTION 2/OPSIE 2 $v_{ave} = \frac{800}{75} \checkmark = 10,67 \text{ m} \cdot \text{s}^{-1}$ $\therefore \text{Distance covered in 1 s} = 10,67 \text{ m}$ $\therefore \text{Work done in 1 s} = (240)(10,67) \checkmark$ $= 2\,560,8 \text{ J s}^{-1}$ $\therefore P_{ave} = 2\,560,8 \text{ W (2,56 kW)} \checkmark$
OPTION 3/OPSIE 3 $P_{ave} = \frac{W}{\Delta E} \checkmark$ $= \frac{F\Delta x \cos \theta}{\Delta E}$ $= \frac{240\Delta \times 800 \cos 0}{75} \checkmark$ $= 2\,560 \text{ W} \checkmark$	

(3)

5.2



Accepted labels/Aanvaarde benoemings	
w	F_g / F_w / weight / mg / gravitational force F_g / F_w / gewig / mg / gravitasiekrag
f	$F_{\text{friction}} / F_f$ / friction F_{wrywing} / F_w / wrywing
N	F_N / F_{normal} / normal force F_N / F_{normaal} / normaalkrag
F_D	$F_{\text{Applied/toegepas}}$ $F_{\text{driving/dryfkrag}}$

(4)

5.3

The net/total work done on an object is equal✓ to the change in the object's kinetic energy ✓

Die netto/totale arbeid verrig op 'n voorwerp is gelyk aan die verandering in die voorwerp se kinetiese energie.

OR/OF

The work done on an object by a resultant/net force is equal✓ to the change in the object's kinetic energy. ✓

Die arbeid verrig op 'n voorwerp deur 'n resulterende krag is gelyk aan die verandering in die voorwerp se kinetiese energie.

(2)

5.4

OPTION 1/OPSIE 1

$$W_{\text{net}} = \Delta K \checkmark$$

$$W_{\text{net}} = W_D + W_g + W_f + W_N \\ = (F_D \Delta x \cos \theta) + (mg \sin \alpha) \Delta x \cos \theta + (f \Delta x \cos \theta) + 0$$

$$W_{\text{net}} = [350(450)](\cos 0^\circ) \checkmark + (300)(9,8) \frac{5}{450} (450)(\cos 180^\circ) \checkmark + \\ 294(450)(\cos 180^\circ) \checkmark \\ = 157\,500 - 14\,700 - 132\,300 \\ = 10\,500 \text{ J}$$

$$W_{\text{net}} = \Delta K$$

$$10\,500 = \frac{1}{2} (300)(v_f^2 - 0) \checkmark$$

$$v_f = 8,37 \text{ m} \cdot \text{s}^{-1} \checkmark$$

OR/OF

$$\alpha = \sin^{-1} \frac{5}{450} \\ = 0,64^\circ$$

(6)

OPTION 2/OPSIE 2

$$W_{\text{nc}} = \Delta U + \Delta K \checkmark$$

$$W_f + W_D = \Delta U + \Delta K$$

$$f \Delta x \cos \theta + W_D = mg(h_f - h_i) + \frac{1}{2} (m)(v_f^2 - v_i^2)$$

$$(f \Delta x \cos \theta + F_D \Delta x \cos \theta = mg(h_f - h_i) + \frac{1}{2} m(v_f^2 - v_i^2)$$

$$(294)(450)(\cos 180^\circ) \checkmark + (350)(450) \cos 0^\circ \checkmark = (300)(9,8)(5 - 0) \checkmark + \frac{1}{2} (300)(v_f^2 - 0) \checkmark \\ v_f = 8,37 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

OPTION 3/OPSIE 3

$$W_{\text{net}} = W_D + W_g + W_f + W_N$$

$$= (F_D \Delta x \cos \theta) + mg \Delta x \cos \theta + f \Delta x \cos \theta + 0$$

$$W_{\text{net}} = (350)(450)(\cos 0^\circ) \checkmark + (300)(9,8)(450) \cos (90 + 0,64) \checkmark + 294(450)(\cos 180^\circ) \checkmark \\ = 157\,500 - 14\,777,74 - 132\,300 \\ = 10\,422,26 \text{ J}$$

$$W_{\text{net}} = \Delta K \checkmark$$

$$10\,422,26 = \frac{1}{2} (300)(v_f^2 - 0) \checkmark$$

$$v_f = 8,34 \text{ m} \cdot \text{s}^{-1} \checkmark$$

OR/OF

$$\alpha = \sin^{-1} \frac{5}{450} \\ = 0,64^\circ$$

(6)

OPTION 4/OPSIE 4

$$F_{\text{net}} = F_D + mg \sin \alpha + f$$

$$= 350 \checkmark - (300)(9,8) \sin 0,64 \checkmark + (-294) \checkmark$$

$$= 350 - 32,84 - 294$$

$$= 23,16 \text{ N}$$

$$W_{\text{net}} = F_{\text{net}} \Delta x \cos \theta$$

$$= (23,16)(450) \cos 0$$

$$= 10\,422 \text{ J}$$

$$W_{\text{net}} = \Delta K \checkmark$$

$$10\,422 = \frac{1}{2} (300)(v_f^2 - 0) \checkmark$$

$$v_f = 8,34 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(6)

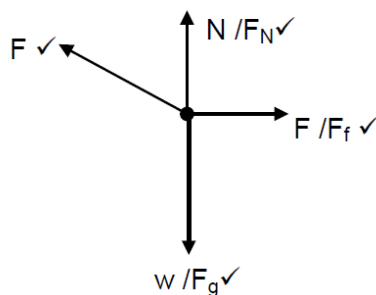
[15]

QUESTION 5/VRAAG 5

5.1 It is a ratio of two forces ✓ (hence units cancel out)./Dit is 'n verhouding van twee kragte ✓ (dus word eenhede uitgekansleer) (1)

5.2 The net work done on an object is equal ✓ to the change in kinetic energy of the object✓/Die netto arbeid wat op 'n voorwerp verrig word, is gelyk ✓ aan die verandering in kinetiese energie van die voorwerp✓ (2)

5.3



(4)

5.4 $F \sin 20^\circ + N = mg$ ✓
 $N = mg - F \sin 20^\circ$

$$\begin{aligned} W_{fk} &= f_k \Delta x \cos \theta = \mu_k N \Delta x \cos \theta \checkmark \\ &= \mu_k (mg - F \sin 20^\circ) (3) \cos \theta \\ &= (0,2) [200(9,8) - F \sin 20^\circ] (3) \cos 180^\circ \checkmark \\ &= (-1176 + 0,205 F) \text{ J} \checkmark \end{aligned} \quad (4)$$

5.5 $W_{\text{tot}} = [W_g] + W_f + W_F \checkmark$
 $0 \checkmark = [0] + [(-1176 + 0,205 F)] + [F (\cos 20^\circ) (3) (\cos 0^\circ)] \checkmark$
 $F = 388,88 \text{ N} \checkmark$

NOTE: Do not penalise if value of W_g is not indicated/

LET WEL: Moenie penaliseer indien die waarde van W_g nie aangedui word nie. (4)
[15]

QUESTION/VRAAG 4

- 4.1 The total mechanical energy in an isolated (closed) system ✓ remains constant (is conserved). ✓
Die totale meganiese energie in 'n geïsoleerde (geslote) sisteem bly konstant (bly behoue).

NOTE/LET WEL

If total or isolated/closed is omitted (max:1/2)

Indien totale of geslote(geïsoleerde) weggelaat is (maks:1/2) (2)

- 4.2 E_{mech} at A = E_{mech} at B / E_{meg} by A = E_{meg} by B ✓

$$(mgh + \frac{1}{2}mv^2)_A = (mgh + \frac{1}{2}mv^2)_B$$

$$m(9,8 \times 0,5 + \frac{1}{2} \times 0^2) \checkmark = m(9,8 \times 0 + \frac{1}{2} \times v^2) \checkmark$$

$$4,9 = \frac{1}{2}v^2$$

$$v = 3,13 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(4)

- 4.3 4.3.1 The net/total work done on an object ✓ is equal to the change in the object's kinetic energy. ✓

Die netto/totale arbeid verrig op 'n voorwerp is gelyk aan die verandering in die kinetiese energie van die voorwerp.

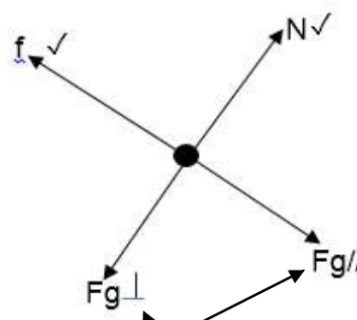
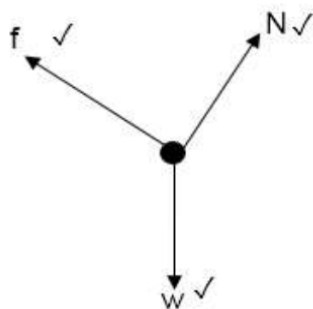
OR/OF

The work done on an object by a resultant/net force is equal ✓ to the change in the object's kinetic energy. ✓

Arbeid verrig deur 'n netto krag is gelyk aan die verandering in die kinetiese energie van die voorwerp.

(2)

4.3.2



✓ for both/vir albei (3)

4.3.3 $W_{\text{net}} = \Delta E_k \checkmark$

$$W_{\text{net}} = 0$$

$$W_f + W_{g//} = 0 \checkmark$$

$$f \cdot \Delta x \cdot \cos \theta + mg \cdot \frac{1}{\Delta x} \Delta x \cdot \cos \theta = 0$$

$$14,7 \cdot d \cdot \cos 180^\circ \checkmark + 3 \times 9,8 \left(\frac{1}{d}\right) \cdot d \cdot \cos 0^\circ = 0$$

$$-14,7d + 29,4 = 0$$

$$d = 2 \text{ m} \checkmark$$

(5)

- 4.4 REMAINS THE SAME/BLY DIESELFDE ✓

(1)

[17]