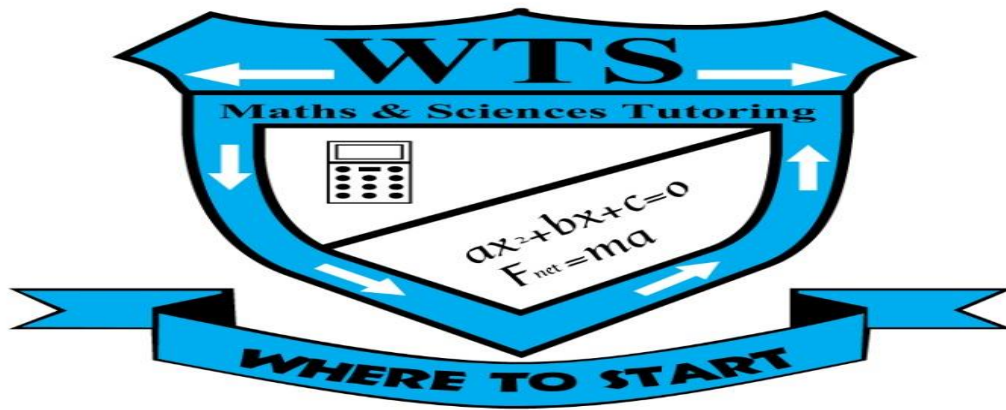


WTS TUTORING



WTS

WORK, ENERGY & POWER MEMO

GRADE : 12

COMPILED BY : PROF KWV KHANGELANI SIBIYA

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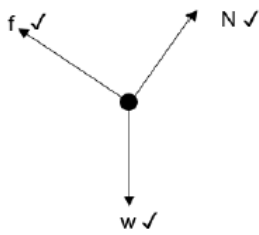
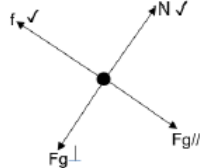
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MEMO FOR PAST PAPERS

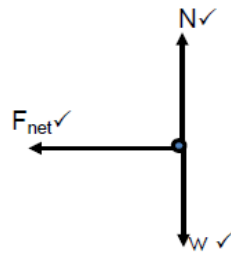
QUESTION/VRAAG 4

4.1	In an <u>isolated system</u> ✓ the total mechanical energy <u>remains constant</u> . ✓ In 'n <u>geïsoleerde sisteem</u> ✓ bly die totale meganiese energie <u>konstant</u> . ✓	(2)
4.2	<p>OPTION 1 / OPSIE 1</p> $\left. \begin{aligned} E_{\text{mech at/by A}} &= E_{\text{mech at/by B}} \\ (mgh + \frac{1}{2}mv^2) \text{ at/by A} &= (mgh + \frac{1}{2}mv^2) \text{ at/by B} \end{aligned} \right\} \begin{array}{l} \checkmark \text{ Any one} \\ \text{Enige een} \end{array}$ $4 \times 9,8 \times (7 \sin 60^\circ) \checkmark + \frac{1}{2} \times 4 \times 0 = 4 \times 9,8 \times (4 \sin 60^\circ) \checkmark + \frac{1}{2} \times 4 \times v^2$ $v = 7,14 \text{ m}\cdot\text{s}^{-1} \checkmark$ <p>OPTION 2 / OPSIE 2</p> $E_{\text{mech at/by A}} = E_{\text{mech at/by B}} \checkmark$ $(mgh + \frac{1}{2}mv^2) \text{ at A} = (mgh + \frac{1}{2}mv^2) \text{ at B}$ $4 \times 9,8 \times (3 \sin 60^\circ) \checkmark + \frac{1}{2} \times 4 \times 0 = 4 \times 9,8 \times (0) \checkmark + \frac{1}{2} \times 4 \times v^2$ $v = 7,14 \text{ m}\cdot\text{s}^{-1} \checkmark$	(4)
4.3	<p>4.3.1 <u>Work done by a net force is equal</u> ✓ to the <u>change in kinetic energy</u> ✓ of an object. OR The <u>net (total) work done</u> ✓ is equal to the <u>change in kinetic energy</u> of the object. ✓ <u>Arbeid verrig deur 'n netto krag is gelyk</u> ✓ aan die <u>verandering in kinetiese energie</u> van 'n voorwerp ✓ OF <u>Die netto (totale) arbeid op 'n voorwerp is gelyk</u> ✓ aan die <u>verandering in kinetiese energie</u> van die voorwerp ✓</p> <p>4.3.2</p> <div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p>✓ for both components of weight ✓ vir albei gewigskomponente</p>	(2)
4.3.3	<p>OPTION 1 / OPSIE 1</p> $\left. \begin{aligned} W_{\text{net}} &= \Delta E_k \\ W_f + W_{g\parallel} &= \frac{1}{2} m(v_f^2 - v_i^2) \end{aligned} \right\} \begin{array}{l} \checkmark \text{ any one} \\ \text{(enige een)} \end{array}$ $f \cdot \Delta x \cdot \cos \theta + m g \sin 60 \cdot \Delta x \cdot \cos \theta = \frac{1}{2} \times 4(3^2 - 7,14^2) \checkmark$ $f \times \frac{2}{\cos 60^\circ} \checkmark \times -1 + 4 \times 9,8 \sin 60 \checkmark \times \frac{2}{\cos 60^\circ} \times 1 = -83,9592$ $-4f + 135,7927833 = -83,9592$ $f = 54,94 \text{ N} \checkmark$ <p>OPTION 2 / OPSIE 2</p> $W_{\text{nc}} = \Delta E_p + \Delta E_k$ $W_f = mgh_f - mgh_i + \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 \left. \vphantom{W_f} \right\} \begin{array}{l} \checkmark \text{ any one / enige een} \end{array}$ $f \cdot \cos \theta \cdot \Delta x = m g (h_f - h_i) + \frac{1}{2} m (v_f^2 - v_i^2) \left. \vphantom{f} \right\}$ $f \cdot \cos 0 \times 4 \checkmark = 4 \times 9,8 (0 - 4 \sin 60^\circ) \checkmark + \frac{1}{2} \times 4 (3^2 - 7,14^2) \checkmark$ $f = 54,94 \text{ N} \checkmark$	(5)
4.4	Remains the same / Bly dieselfde ✓	(1)

[17]

QUESTION / VRAAG 3

3.1



(3)

$$3.2 \quad 120 \text{ kmh}^{-1} = \frac{120 \times 1000}{3600} = 33,33 \text{ m}\cdot\text{s}^{-1} \quad \checkmark$$

(1)

3.3 **Work-energy theorem:** The net work done on an object is equal to the change in the objects kinetic energy. $\checkmark\checkmark$

Arbeid energie beginsel: Die netto arbeid verrig op 'n voorwerp is gelyk aan die verandering in die voorwerp se kinetiese energie.

(2)

$$3.4 \quad 3.4.1 \quad W_{\text{net}} = E_{\text{kf}} - E_{\text{ki}} \checkmark$$

$$= 0 - \frac{1}{2}mv^2$$

$$= 0 - \frac{1}{2}(1000) \times 33,33^2 \checkmark$$

$$= -555\,444,45 \text{ J}$$

$$F_{\text{net}}\Delta x \cos\theta = 555\,444,45 \checkmark$$

$$F_{\text{net}}(0,8)\cos 180^\circ = 555\,444,45$$

$$F_{\text{net}} = -694\,305,56 \text{ N}$$

$$F_{\text{net}} = 694\,305,56 \text{ N to the left} \checkmark / \text{away from the}$$

wall/opposite direction of initial motion

Na links / weg van die muur / teenoorgestelde rigting van die aanvanklike beweging

(5)

$$3.4.2 \quad \text{Time lapse / Tydperk} \quad F_{\text{net}} \Delta t = \Delta p = m(v_f - v_i) \checkmark$$

$$\Delta t = \frac{1\,000(0 - 33,33)}{-694\,305,56} \checkmark\checkmark$$

$$= 0,05 \text{ s} \checkmark$$

(4)

3.4.3

- Crumbling increases stopping time \checkmark / *frommeling vergroot stop-tyd*
- thus reducing F_{net} \checkmark / *dus verminder F_{net}*

$$\bullet \quad F_{\text{net}} = \frac{\Delta p}{\Delta t} \checkmark$$

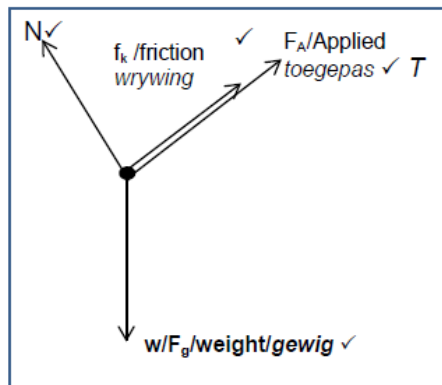
(3)

[18]

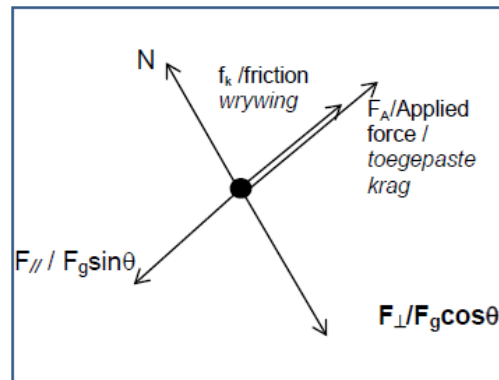
QUESTION / VRAAG 4

4.1

Option 1 / Opsie 1



Option 2 / Opsie 2



(4)

Accepted labels/Aanvaarde benoemings	
w	F_g/F_w /weight/mg/gravitational force F_g/F_w /gewicht/mg/gravitasiekrag
f	F_{friction}/F_f /friction/ f_k F_{wrywing}/F_w /wrywing/ f_k
N	F_N/F_{normal} /normal force F_N/F_{normaal} /normaalkrag
	Deduct 1 mark for any additional force. / Trek een punt af vir enige ekstra krag
	Mark is given for both arrow and label. / Punt word toegeken vir beide 'n pyl en byskrif.

4.2 0 N ✓

Box slides at constant velocity / $\Delta E_k = 0$ / acceleration = 0 ✓
 Boks gly teen konstante snelheid / versnelling = 0

(2)

4.3 A non-conservative force is that force for which the work done in moving an object between two points depends on the path taken.
 'n Nie-konserwatiewe krag is daardie krag waarvan die arbeid verrig afhang van die padlengte gevolg tussen twee punte.

(2)

$$4.4 \quad \theta = \sin^{-1} \frac{1,2}{6} \checkmark = 11,537^\circ$$

Option 1 / Opsie 1

$$W_{\text{nett}} = \Delta E_k \checkmark$$

$$W_A + W_f + W_N + W_\perp + W_\parallel = 0 \checkmark$$

$$W_A + F_f \Delta x \cos 180 + 0 + 0 + 100 \times 9,8 \sin 11,537^\circ \times 6 \cos 0 \checkmark = 0$$

$$W_A + 60 \times 6 \cos 180 \checkmark + 100 \times 9,8 \sin 11,537^\circ \times 6 \cos 0 = 0$$

$$W_A = -816 \text{ J}$$

$$\underline{\text{Work done by man} = 816 \text{ J} \checkmark}$$

Arbeid verrig deur man

Option 2 / Opsie 2

$$F_{\text{nett}} = F_A + f + F_\parallel + N + F_\perp$$

$$= F_A + f + F_\parallel$$

$$0 = F_A - 60 + 100 \times 9,8 \times \sin 11,537^\circ$$

$$= F_A + 136$$

$$F_A = -136 \text{ N}$$

$$\therefore W_A = F_A \times \Delta x$$

$$= -136 \times 6$$

$$= -816 \text{ J}$$

$$\therefore \underline{\text{work done by man is 816 J} \checkmark}$$

Arbeid verrig deur man

Option 3 / Opsie 3

$$W_{\text{nc}} = \Delta E_k + \Delta E_p$$

$$W_{\text{man}} + W_f = 0 + mg(h_f - h_i)$$

$$W_{\text{man}} + 60 \times 6 \times (-1) = 100 \times 9,8 (0 - 1,2)$$

$$W_{\text{man}} = -1176 + 360$$

$$= -816 \text{ J}$$

$$\therefore \underline{\text{work done by man is 816 J}}$$

Arbeid verrig deur man

(6)

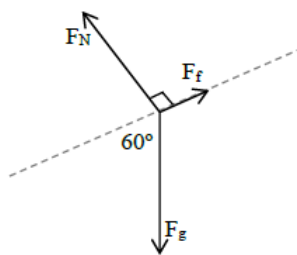
$$\begin{aligned}
 4.5 \quad W_A &= F \Delta x \cos \theta \checkmark = -816 \\
 &= F \times 6 \cos 180 \checkmark = -816 \checkmark \\
 F_A &= 136 \text{ N}
 \end{aligned}$$

Magnitude of force applied by man is 136 N. ✓
Grootte van krag toegepas deur man is 136 N

(4)
[18]

QUESTION 5

5.1



F_g = gravitational force or weight ✓
 F_N = Normal force ✓
 F_f = frictional force ✓

(3)

$$5.2 \quad W_{\text{net}} = F_{\text{net}} \Delta x \cos \theta \checkmark = (F_{\text{gll}} + (-F_f)) \Delta x = (343 \checkmark - 150 \checkmark)(120 \checkmark) = 23160 \text{ J} \checkmark \quad (5)$$

5.3 The work done by a net force ✓ on an object is equal to the change in the kinetic energy ✓ of the object.

OR

Net work done ✓ on an object is equal to the change in the kinetic energy ✓ of the object. (2)

Mark positively from 5.2

$$\begin{aligned}
 5.4 \quad W_{\text{net}} &= \Delta E_k \checkmark = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 \\
 23160 \checkmark &= \frac{1}{2} (70) v_f^2 - 0 \checkmark \\
 v_f &= 25,72 \text{ m.s}^{-1} \checkmark
 \end{aligned}$$

(4)
[14]

QUESTION 5 // VRAAG 5

5.1



NB: See Question 2.5 for NOTES and Accepted labels!

LW! Sien VRAAG 2.5 vir NOTAS en aanvaarbare byskrifte

(2)

5.2 Gravitational force✓ // Gravitatiekrak

(1)

5.3 The net/total work done on an object is equal✓ to the change in the object's kinetic energy.✓ // die netto/totale arbeid op 'n voorwerp verrig is gelyk aan die verandering in die voorwerp se kinetiese energie.

OR // OF:

The work done on an object by a net/resultant force is equal to the change in the object's kinetic energy.// die arbeid op 'n voorwerp verrig deur 'n netto/resultante krag is gelyk aan die verandering in die voorwerp se kinetiese energie. (2)

5.4 Take clockwise as positive // Vat klokgewys as positief

For block B // vir blok B:



$$F_{\text{net}} = ma$$

$$W + (-T)m = ma$$

$$mg - T = ma \quad \checkmark$$

$$(10)(9,8) - T = 10 \cdot a \quad \checkmark$$

$$98 - T = 10 \cdot a \dots (1)$$

For block A // vir blok A :



$$F_{\text{net}} = ma$$

$$\therefore T = (-W) = ma$$

$$\therefore T - mg = ma$$

$$\therefore T - (4,0)(9,8) = (4,0) \cdot a \quad \checkmark$$

$$\therefore T - 39,2 = (4,0) \cdot a \dots (2)$$

$$\therefore 98 - T = (10) a \dots (1)$$

$$\therefore -39,2 + T = (4,0) a$$

$$(1) + (2) : 58,8 = (14) a$$

$$\therefore a = 4,2 \text{ m} \cdot \text{s}^{-2}$$

$$\text{From (2): } T - 39,2 = (4,0)(4,2)$$

$$\therefore T - 39,2 = 16,8$$

$$\therefore T = 56 \text{ N} \quad \checkmark$$

$$W_{\text{net}} = \Delta k \checkmark$$

$$W_w + W_T = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$mg \cdot \Delta x \cdot \cos \theta + T \cdot \Delta x \cdot \cos \beta = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$(10)(9,8)(4,0)(\cos 0^\circ) + (56)(4,0)(180^\circ) \checkmark = \frac{1}{2}(10)v_f^2 - 0 \checkmark$$

$$392 + (-224) = 5v_f^2$$

$$1,68 = 5v_f^2$$

$$\therefore v_f^2 = 33,6$$

$$\therefore v_f = \sqrt{33,6} = 5,797 \text{ m} \cdot \text{s}^{-1} \quad (7)$$

5.5 POSITIVE MARKING FROM QUESTION 5.4 // positiewe nasien vanaf VRAAG 5.4:

$$\Delta t(\mathbf{A}) = \Delta t(\mathbf{B})$$

$$\therefore v_f = v_i + \cdot \Delta t \checkmark$$

$$5,797 = 0 + (4,2) \cdot \Delta t \checkmark$$

$$\therefore \Delta t = 1,38 \text{ s} \checkmark \quad (3)$$

[15]

QUESTION 4 / VRAAG 4

4.1 The energy that an object has due to its height above the ground / a reference point ✓✓

Die energie wat 'n voorwerp het as gevolg van die hoogte bo die grond / bo 'n verwysingspunt. (2)

4.2.1 $E_p = mgh \checkmark$

$$= (5,05)(9,8)(0,06) \checkmark$$

$$= 2,97 \text{ J} \checkmark \quad (3)$$

4.2.2 **USE ENERGY PRINCIPLES ONLY. ANY OTHER METHOD: 0/4**

POSITIVE MARKING FROM Q4.2

$$(mgh + \frac{1}{2}mv^2)_R = (mgh + \frac{1}{2}mv^2)_S \checkmark$$

$$0 + \frac{1}{2}(5,05)v^2 \checkmark = 2,97 \checkmark + 0$$

$$v = 1,08 \text{ m} \cdot \text{s}^{-1} \checkmark$$

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$(5,05 \times 9,8)(0,06) \cos 180^\circ \checkmark = 0 - \frac{1}{2}(5,05)v^2 \checkmark$$

$$v = 1,08 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(4)

4.2.3 **POSITIVE MARKING FROM Q4.3**

$$\Sigma p_i = \Sigma p_f$$

$$(mv_i)_1 + (mv_i)_2 = (m_1 + m_2)v_f \quad \left. \vphantom{(mv_i)_1 + (mv_i)_2 = (m_1 + m_2)v_f} \right\} \text{Any one } \checkmark$$

$$(0,05)v_i + 0 \checkmark = (5,05)(1,08) \checkmark$$

$$v_i = 109,08 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(4)

[13]

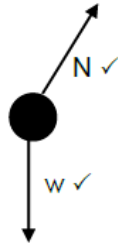
QUESTION 5 / VRAAG 5

- 5.1 The contact force which a surface exerts on an object ✓ and which is perpendicular to the surface. ✓

Die kontakkrag wat 'n oppervlak op 'n voorwerp uitoefen en wat loodreg op die oppervlak is.

(2)

5.2



(2)

Accepted labels / Aanvaarde benoemings	
w	F_g / F_w /force of earth on block/weight / 49 N / mg / gravitational force
N	Normal force / F_N / Force of incline on trolley

5.3

OPTION 1

$$(mgh + \frac{1}{2}mv^2)_X = (mgh + \frac{1}{2}mv^2)_Y \checkmark$$

$$\frac{(76)(9,8)(1,5)}{v} + \frac{1}{2}(76)(3)^2 \checkmark = 0 + \frac{1}{2}(76)v^2 \checkmark$$

$$v = 6,2 \text{ m}\cdot\text{s}^{-1} \checkmark$$

OPTION 2

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$W_w = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

$$(76 \times 9,8)(1,5) \cos 0^\circ \checkmark = \frac{1}{2}(76)v_f^2 - \frac{1}{2}(76)(3)^2 \checkmark$$

$$v_f = 6,2 \text{ m}\cdot\text{s}^{-1} \checkmark$$

OPTION 3

$$W_{\text{nc}} = \Delta E_k + \Delta E_p \checkmark$$

$$0 = (\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2) + (mgh_f - mgh_i)$$

$$0 = [\frac{1}{2}(76)v_f^2 - \frac{1}{2}(76)(3)^2] \checkmark + [0 - (76)(9,8)(1,5)] \checkmark$$

$$v_f = 6,2 \text{ m}\cdot\text{s}^{-1} \checkmark$$

(4)

5.4

$$f_k = \mu_k \cdot N \checkmark$$

$$= \mu_k \cdot mg \cos \Theta$$

$$= (0,21)(76 \times 9,8 \times \cos 10^\circ) \checkmark$$

$$= 154,03 \text{ N} \checkmark$$

(3)

5.5

The normal force is perpendicular to the displacement / motion. ✓

OR

$$\Theta = 90^\circ \rightarrow \cos 90^\circ = 0 \checkmark$$

OR

$$W_N = N \Delta x \cos 90^\circ = 0 \checkmark$$

(1)

5.6 POSITIVE MARKING FROM Q5.3

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$W_{\text{w/l}} + W_f = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

$$(76 \times 9,8 \times \sin 10^\circ)(\Delta x) \cos 0^\circ \checkmark + (154)(\Delta x) \cos 180^\circ \checkmark = 0 - \frac{1}{2}(76)(6,2)^2 \checkmark$$

$$129,33\Delta x - 154\Delta x = -1460,72$$

$$\Delta x = 59,22 \text{ m}$$

$$h = \Delta x \sin 10^\circ$$

$$= 59,22 \sin 10^\circ \checkmark$$

$$= 10,28 \text{ m} \checkmark$$

(6)

5.7 Remains the same \checkmark

(1)

[19]

QUESTION 5 / VRAAG 5

- 5.1 The total mechanical energy remains constant/is conserved \checkmark in
an isolated/closed system. \checkmark
Die totale meganiese energie bly konstant/bly behoue \checkmark in 'n
geïsoleerde/ geslote sisteem \checkmark

OR/OF

The sum of the potential and kinetic energy remains constant \checkmark in
an isolated/closed system. \checkmark
Die som van die potensiële en kinetiese energie bly konstant \checkmark in
'n geïsoleerde / geslote sisteem \checkmark

OR/OF

When the work done by the non-conservative forces is zero✓
the total mechanical energy of the system of bodies is conserved✓.

Wanneer die werk wat gedoen is deur die nie-konserwatiewe kragte nul is✓, is die totale meganiese energie van die stelsel van liggame behoue✓.

(2)

Notes/Aantekeninge:

The mark for 'closed/isolated system' is only awarded if used in conjunction with energy

Die punt vir 'geslote/geïsoleerde sisteem' word slegs toegeken indien saam met energie gebruik

5.2

$$\begin{aligned}
 K_i + U_i &= K_f + U_f \\
 \frac{1}{2}mv^2 + mgh &= \frac{1}{2}mv^2 + mgh \\
 0 + (40)(9.8)(1.5) &= \frac{1}{2}(40)v^2 + 0 \\
 v &= 5.42 \text{ m} \cdot \text{s}^{-1}
 \end{aligned}$$

Notes/ Aantekeninge
Accept/ Aanvaar

E_p and E_k

(4)

5.3

Option 1/Opsie 1

$$\begin{aligned}
 W_{net} &= \Delta K \\
 mg\Delta x \cos\theta + f\Delta x \cos\theta &= \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 \\
 (22)(9.8)(3) \cos 60^\circ + (1.9)(3) \cos 180^\circ &= \frac{1}{2}(22)(v_f^2 - 0^2) \\
 v_f &= 5.37 \text{ m} \cdot \text{s}^{-1}
 \end{aligned}$$

Accept/
Aanvaar

$\Delta y / \Delta x$

Option 2/Opsie 2

Accept/
Aanvaar

$w_{net} = \Delta K \checkmark$ $mg \sin \theta \Delta x \cos \theta + f \Delta x \cos \theta = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$ $(22)(9.8) \sin 30^\circ (3) \cos 0^\circ \checkmark + (1.9)(3) \cos 180^\circ \checkmark = \frac{1}{2} (22)(v_i^2 - 0^\circ) \checkmark$ $v_f = 5,37 m \cdot s^{-1} \checkmark$	$\Delta y / \Delta x$
Option 3/Opsie 3 $w_{net} = \Delta K \checkmark$ $mgh \cos \theta + f \Delta x \cos \theta = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$ $(22)(9.8)(1.5) \cos 0^\circ \checkmark + (1.9)(3) \cos 180^\circ \checkmark = \frac{1}{2} (22)(v_i^2 - 0^\circ) \checkmark$ $v_f = 5,37 m \cdot s^{-1} \checkmark$	Accept/ Aanvaar h / Δy / Δx
$w_{net} = \Delta K \checkmark$ $-\Delta U + f \Delta x \cos \theta = \frac{1}{2} m v^2 - \frac{1}{2} m v^2$ $-(0 - (22)(9.8)(1.5)) \checkmark + (1.9)(3) \cos 180^\circ \checkmark = \frac{1}{2} (22)(v_i^2 - 0^\circ) \checkmark$ $v_f = 5,37 m \cdot s^{-1} \checkmark$	Accept/ Aanvaar h / Δy / Δx

(5)

5.4 Equal to / Gelyk aan \checkmark (1)
[12]

QUESTION 5/VRAAG 5

- 5.1 The force which a surface exerts on an object with which it is in contact✓ and which is perpendicular to the surface.✓
Die krag wat 'n oppervlak uitoefen op 'n voorwerp waarmee dit in kontak is en wat loodreg op die voorwerp is. (2)

5.2
$$\begin{aligned} F_{\text{net}} &= ma \\ F_{\text{applied}} - F_{g//} &= ma \end{aligned} \quad \checkmark$$

$$600\checkmark - m(9,8)(\sin 25^\circ) \checkmark = 0\checkmark$$

$$m = 144,87 \text{ kg}\checkmark$$
 (5)

- 5.3 Total mechanical energy in a closed system✓ remains constant. ✓
Totale meganiese energie in 'n geslote sisteem bly konstant. (2)

5.4.1 **POSITIVE MARKING FROM 5.2/POSITIEWE NASIEN VANAF 5.2**

OPTION 1/ OPSIE 1

$$(E_p + E_k)_X = (E_p + E_k)_B \checkmark$$

$$(144,87)(9,8)h \checkmark + 0 = 0 + \frac{1}{2}(144,87)(6)^2 \checkmark$$

$$h = 1,84 \text{ m}\checkmark$$

OPTION 2/ OPSIE 2

$$W_{\text{nc}} = \Delta U + \Delta K \checkmark / W_{\text{nc}} = \Delta E_p + \Delta E_k$$

$$0 = \frac{0 - (144,87)(9,8)(5)h \checkmark + \frac{1}{2}(144,87)(6)^2 - 0\checkmark}{h = 1,84 \text{ m}\checkmark}$$
 (4)

5.4.2 **POSITIVE MARKING FROM 5.2/POSITIEWE NASIEN VANAF 5.2**

OPTION 1/ OPSIE 1

$$\begin{aligned} W_{\text{net}} &= \Delta K \checkmark \\ W_f &= \Delta K \checkmark \end{aligned}$$

$$\mu_k(144,87)(9,8)\checkmark(5)\cos 180^\circ \checkmark = \frac{1}{2}(144,87)2^2 - \frac{1}{2}(144,87)(6^2) \checkmark$$

$$\mu_k = 0,33 \checkmark$$

OPTION 2/ OPSIE 2

$$\begin{aligned} W_{\text{nc}} &= \Delta U + \Delta K \checkmark \\ W_f &= \Delta U + \Delta K \checkmark \end{aligned}$$

$$\mu_k(144,87)(9,8)\checkmark(5)\cos 180^\circ \checkmark = 0 + \frac{1}{2}(144,87)2^2 - \frac{1}{2}(144,87)(6^2) \checkmark$$

$$\mu_k = 0,33 \checkmark$$
 (5)

[18]

QUESTION / VRAAG 4

- 4.1 The total (linear) momentum of a closed system remains constant/is conserved. ✓✓
(2 marks or zero)

Die totale (liniêre) momentum van 'n geslote sisteem bly konstant/bly behoue. ✓✓
(2 punte or niks) (2)

- 4.2 $\Sigma p_i = \Sigma p_f$ ✓
 $m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_c$
 $(68 \times 20) + (12 \times 0) = (68 + 12) v_c$ ✓
 $\therefore v_c = 17 \text{ m} \cdot \text{s}^{-1}$ ✓ (4)

- 4.3 **POSITIVE MARKING FROM QUESTION 4.2 / POSITIEWE NASIEN VAN VRAAG 4.2.**

OPTION / OPSIE 1

$$(E_p + E_k)_i = (E_p + E_k)_f \checkmark$$

$$(mgh + \frac{1}{2}mv_c^2)_i = (mgh + \frac{1}{2}mv_c^2)_f$$

$$0 + \frac{1}{2}(80)(17)^2 = (80)(9,8)h + 0 \checkmark$$

$$\therefore h = 14,75 \text{ m}$$

Distance up the incline, d/ *Afstand opwaarts teen skuinsvlak*

$$\sin \theta = \frac{h}{\Delta x}$$

$$\sin 25^\circ = \frac{14,75}{\Delta x} \checkmark$$

$$\therefore \Delta x = 34,89 \text{ m} \checkmark$$

OPTION / OPSIE 2

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$W_w = E_{kf} - E_{ki}$$

$$mgsin 25^\circ \cos 180^\circ = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$(80)(9,8)\sin 25^\circ \cos 180^\circ = \frac{1}{2}(80)(0^2 - 17^2) \checkmark$$

$$\Delta x = 34,89 \text{ m} \checkmark$$

(5)

- 4.4 Decreases / *verminder* ✓

Friction is a non-conservative force/ opposes motion/removes kinetic energy from the system. ✓

Wrywing is 'n nie-konserwatiewe krag /opponeer beweging / verwyder kinetiese energie van die sisteem. ✓

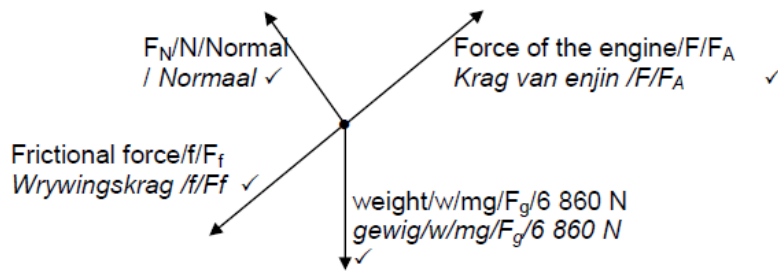
(2)

[13]

QUESTION / VRAAG 5

5.1 Zero/0 (J) ✓ (1)

5.2



(4)

5.3 5.3.1 The net/total work done on an object is equal to the change in the object's kinetic energy. ✓✓ (2 marks or zero.)

Die netto/totale werk verrig op 'n voorwerp is gelyk aan die verandering in die voorwerp se kinetiese energie. ✓✓ (2 punte or niks.)

(2)

5.3.2 **Marking guidelines / nasienriglyne**

- Formula/ Formule: $W_{\text{net}} = \Delta E_k$ or $W_{\text{nc}} = \Delta E_p + \Delta E_k$ ✓
- Formula / Formule: $W = F \Delta x \cos \theta$ ✓
- Substitution to calculate / Vervanging in formule $f = \mu_k mg \cos 30^\circ$ ✓
- Substitute to calculate / Vervanging om te bereken: W_f ✓
- Substitute to calculate / Vervanging om te bereken: W_w OR ΔE_p ✓
- Substitute to calculate / Vervanging om te bereken: W_F ✓
- Substitute to calculate / Vervanging om te bereken: ΔE_k ✓
- Final answer / Finale antwoord: $11,59 \text{ m} \cdot \text{s}^{-1}$ ✓

OPTION / OPSIE 1:

$$W_{\text{net}} = \Delta E_k \checkmark$$

$$W_N + W_f + W_w + W_F = \Delta E_k$$

$$0 + f \Delta x \cos 180^\circ + w \Delta x \cos 180^\circ + F \Delta x \cos 0^\circ \checkmark = E_{kf} - E_{ki}$$

$$\mu_k mg \cos 30^\circ \Delta x \cos 180^\circ + mg \Delta x \sin 30^\circ \cos 180^\circ + F \Delta x \cos 0^\circ = \frac{1}{2} m(v_f^2 - v_i^2)$$

$$0,32(700)(9,8) \cos 30^\circ \checkmark (70) \cos 180^\circ \checkmark + (700)(9,8) \sin 30^\circ (70) \cos 180^\circ \checkmark + (6000)(70) \cos 0^\circ \checkmark = \frac{1}{2} (700)(v_f^2 - 0) \checkmark$$

$$-1,33 \times 10^5 - 2,4 \times 10^5 + 4,2 \times 10^5 = 350 v_f^2$$

$$v_f = 11,59 \text{ m} \cdot \text{s}^{-1} \checkmark$$

OPTION / OPSIE 2:

$$W_{\text{nc}} = \Delta E_p + \Delta E_k \checkmark$$

$$W_f + W_F = mg \Delta h + \frac{1}{2} m(v_f^2 - v_i^2)$$

$$f \Delta x \cos 180^\circ + F \Delta x \cos 0^\circ \checkmark = mg \Delta h + \frac{1}{2} m(v_f^2 - v_i^2)$$

$$0,32(700)(9,8) \cos 30^\circ \checkmark (70) \cos 180^\circ \checkmark + (6000)(70) \cos 0^\circ \checkmark =$$

$$(700)(9,8)(70 \sin 30^\circ - 0) \checkmark + \frac{1}{2} (700)(v_f^2 - 0) \checkmark$$

$$v_f = 11,59 \text{ m} \cdot \text{s}^{-1} \checkmark$$

(8)

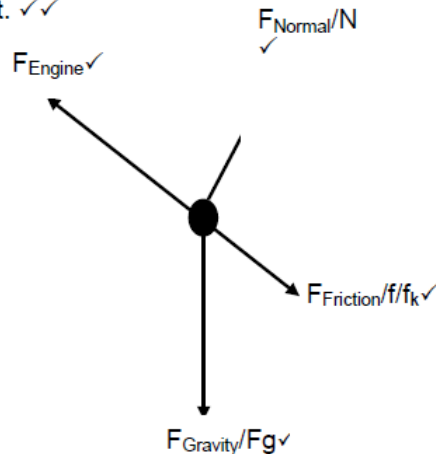
[15]

QUESTION 5

- 5.1 Net work done on an object is equal to the change in the kinetic energy of the object. ✓✓

(2)

5.2



-1 for additional forces
Direction and label
must be correct

(4)

5.3

$$\begin{aligned}
 f_k &= \mu_k N \quad \checkmark \\
 &= (0,017) \checkmark (1500)(9,8)(\cos 10,21^\circ) \checkmark \\
 &= 245,94 \text{ N}
 \end{aligned}$$

(3)

5.4

$$\begin{aligned}
 \sin 10,21 &= 59/AB \\
 AB &= 332,85 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 W_{\text{net}} &= \Delta E_k \checkmark \\
 W_{F_e} + W_N + W_{F_f} + W_{F_{g\perp}} + W_{F_{gp}} &= 0 \checkmark \\
 F_e \Delta x \cos \theta + 0 + F_f \Delta x \cos \theta + 0 + F_{gp} \Delta x \cos \theta &= 0 \\
 F_e(332,85)(\cos 0^\circ) \checkmark + (245,94)(332,85)(\cos 180^\circ) \checkmark + m g \sin \theta \Delta x \cos \theta &= 0 \\
 332,85 F_e - 81861,13 + (1500)(9,8)(\sin 10,21^\circ)(332,85)(\cos 180^\circ) \checkmark &= 0 \\
 332,85 F_e &= 949158,63 \\
 F_e &= 2851,61 \text{ N} \\
 P &= F \cdot v \checkmark \\
 &= (2851,61)(10) \\
 &= 28516,10 \text{ W} \checkmark \text{ (Accept: } 28\,539,33 \text{ W)}
 \end{aligned}$$

(7)

OR

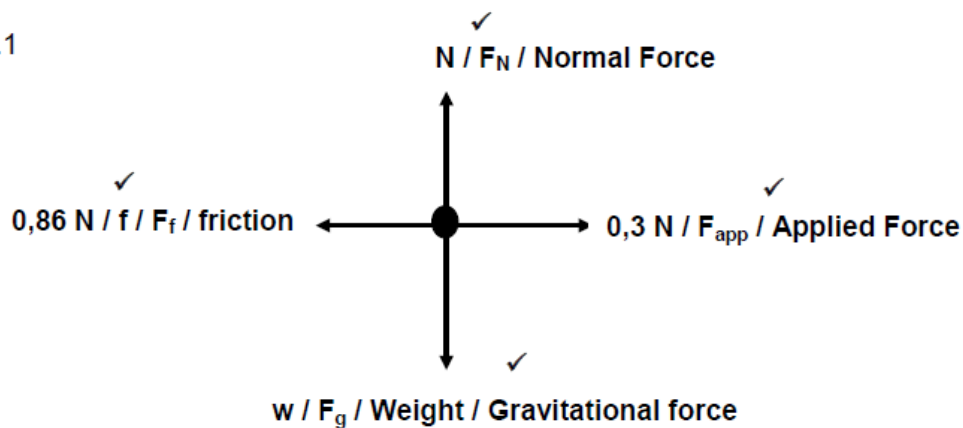
$$\begin{aligned}
 W_{\text{nc}} &= \Delta E_p + \Delta E_k \checkmark \\
 W_f + W_{F_e} &= mg \Delta h + 0 \checkmark \\
 F_f \Delta x \cos \theta + F_e \Delta x \cos \theta &= (1500)(9,8)(59) \checkmark \\
 (245,94)(332,85)(-1) \checkmark + 332,85 F_e \checkmark &= 867300 \\
 F_e &= 2851,62 \text{ N} \\
 P &= F \cdot v \checkmark \\
 &= (2851,62)(10) \\
 &= 28516,20 \text{ W} \checkmark
 \end{aligned}$$

(7)

1161

QUESTION 4

4.1



(4)

4.2 $F_{\text{net}} = F_{\text{applied}} + F_f = 0,30 + (-0,86) = -0,56 \text{ N} = 0,56 \text{ N}$ opposite direction of motion/ to the left (3)

4.3 Work Energy theorem states that, the net/total work done on an object is equal to the change in the object's kinetic energy. (2)

OR

the work done on an object by a resultant/net force is equal to the change in the object's kinetic energy.

4.4

$$\begin{aligned}
 W_{\text{NET}} &= \Delta E_K \\
 F_{\text{net}} \Delta x \cos \theta &= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 \\
 0,56 \Delta x \cos 180 &= \frac{1}{2} (0,8) (0,2)^2 - \frac{1}{2} (0,8) (1,2)^2 \\
 (0,56) \times (\Delta x) \times (-1) &= 0,016 - 0,576 \\
 \Delta x &= 1 \text{ m}
 \end{aligned}$$

OR

$$\begin{aligned}
 W_{\text{NC}} &= \Delta E_K + \Delta E_P \\
 f \Delta x \cos 180 + F_{\text{APPL}} \Delta x \cos 0 &= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 + 0 \\
 0,86 \cdot \Delta x \cos 180 + 0,3 \cdot \Delta x \cos 0 &= \frac{1}{2} (0,8) (0,2)^2 - \frac{1}{2} (0,8) (1,2)^2 \\
 (-0,86 + 0,3) \cdot \Delta x &= 0,016 - 0,576 \\
 \Delta x &= 1 \text{ m}
 \end{aligned}$$

(4)

4.5 Friction **OR** applied force (note: symbols not accepted) (1)

[14]

QUESTION 5

- 5.1 The net (total) work done on an object ✓ is equal to the change in the object's kinetic energy. ✓ **OR**
 The work done on an object by a net (resultant) force ✓ is equal to the change in the object's kinetic energy. ✓

(2)

5.2 $W_g = F_g \Delta y \cos \theta$ ✓
 $= mg \Delta y \cos \theta$
 $= (75)(9,8)(2,4 - 1,6) \cos 0^\circ$ ✓
 $= 588 \text{ J}$ ✓

OR

work due to a conservative forces is equal to negative change in potential energy associated with that conservative force:

$$W_c = -\Delta E_p$$

$$W_g = -mg(h_f - h_i)$$

$$= -(75)(9,8)(1,6 - 2,4)$$

$$= 588 \text{ J}$$

(4)

5.3

$$W_{\text{net}} = \Delta E_k$$

$$W_f + W_g = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

$$W_f + 588 = \frac{1}{2}(75)(3,75^2 - 0^2)$$

$$W_f = -60,66 \text{ J}$$

OR

$$W_{\text{nc}} = \Delta E_p + \Delta E_k$$

$$W_f = mg(h_f - h_i) + \frac{1}{2}m(v_f^2 - v_i^2)$$

$$= (75)(9,8)((1,6 - 2,4)) + \frac{1}{2}(75)((3,75^2 - 0^2))$$

$$= -60,66 \text{ J}$$

(6)

5.4.1 REMAINS THE SAME ✓

(1)

- 5.4.2 The gravitational force is conservative (non-contact) force ✓, so the work done by the gravitational force will not depend on the path taken. ✓ The starting and ending points are the same. Therefore the work done by the gravitational force will remain the same.

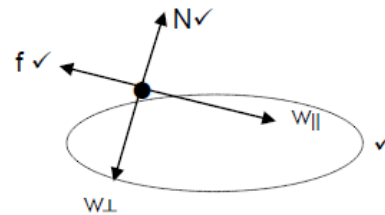
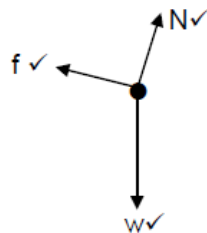
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[15]

QUESTION 5/VRAAG 5

5.1

Accepted Labels/Aanvaarde benoemings	
w	F_g/F_w /force of Earth on crate/weight/39,2 N/mg/gravitational force F_g/F_w /krag van Aarde op krat/gewig/39,2 N/mg/gravitasiekrag
f	f / friction f / wrywing
N	Normal force / F_N / Force of surface on block Normale krag / F_N / Krag van oppervlak op blok



Notes / Aantekeninge

- Any additional forces max $\frac{2}{3}$
Enige addisionel kragte maks $\frac{2}{3}$
- No arrows max $\frac{2}{3}$
Geen pylpunte maks $\frac{2}{3}$
- Forces not touching dot max $\frac{2}{3}$
Kragte wat nie kolletjie raak nie maks $\frac{2}{3}$

(3)

5.2

The net/total work done on an object is equal to the change in the object's kinetic energy. ✓✓

Die netto / totale arbeid verrig op 'n voorwerp is gelyk aan die verandering in kinetiese energie van die voorwerp

OR/OF

The work done on an object by a resultant/net force is equal to the change in the object's kinetic energy. ✓✓

Die arbeid verrig op 'n voorwerp deur 'n resulterende / netto krag is gelyk aan die verandering in kinetiese energie van die voorwerp .

(2)

5.3 **Incline/Skuinsvlak**

$$W_{fk} = f_k \Delta x \cos \theta \quad \checkmark = \mu_k N \Delta x \cos \theta \quad \checkmark = \mu_k (mg \cos 30^\circ) \Delta x \cos 180^\circ \quad \checkmark$$

$$= (0,2)(4)(9,8) \cos 30^\circ (3)(-1) \quad \checkmark$$

$$= -20,3689 \text{ J}$$

$$W_w = w \Delta x \cos 60^\circ = (4)(9,8)(3) \cos 60^\circ = 58,8 \text{ J}$$

$$W_{\text{net}} = \Delta K = K_f - K_i \quad \checkmark$$

$$W_w + W_N + W_f = K_f - 0$$

$$58,8 + 0 - 620,3689 \quad \checkmark = K_f$$

$$K_f = 38,431 \text{ J} \quad \checkmark$$

Horizontal surface/Horisontale opplervlak

$$W_{\text{net}} = \Delta K$$

$$W_w + W_N + W_f = K_f - K_i$$

$$0 + 0 + \mu_k N \Delta x \cos \theta = 0 - 38,431$$

$$(0,5)(4)(9,8) \Delta x \cos 180^\circ = -38,431 \quad \checkmark$$

$$\Delta x = 1,96 \text{ m} \quad \checkmark$$

(8)

[16]

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