



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE/ *NASIONALE SENIOR SERTIFIKAAT*

GRADE/GRAAD 10

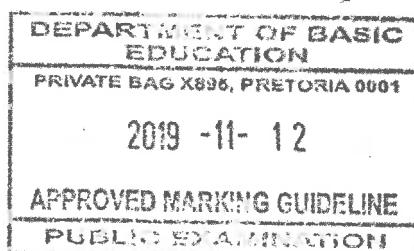
MATHEMATICS P1/WISKUNDE VI

NOVEMBER 2019

MARKING GUIDELINES/NASIENRIGLYNE

MARKS/PUNTE: 100

These marking guidelines consist of 13 pages./
Hierdie nasienriglyne bestaan uit 13 bladsye.



K.C.
12/11/19

NOTE:

- If a candidate answered a *QUESTION* TWICE, mark only the FIRST attempt.
- If a candidate crossed out an answer and did not redo it, mark the crossed-out answer.
- Consistent accuracy applies to ALL aspects of the marking guidelines.
- Assuming values/answer in order to solve a problem is unacceptable.

LET WEL:

- As 'n kandidaat 'n vraag TWEE keer beantwoord het, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord deurgehaal en nie oorgedoen het nie, sien die deurgehaalde antwoord na.
- Volgehoue akkuraatheid is op ALLE aspekte van die nasienriglyne van toepassing.
- Dit is onaanvaarbaar om waardes/antwoorde te veronderstel om 'n probleem op te los.

QUESTION/VRAAG 1

1.1.1	$\begin{aligned}3y^2 + y \\= y(3y+1)\end{aligned}$	✓ answer/antwoord (1)
1.1.2	$\begin{aligned}x^2 - 10x - 24 \\= (x-12)(x+2)\end{aligned}$	✓ $(x-12)$ ✓ $(x+2)$ (2)
1.1.3	$\begin{aligned}9x^2 - y^2 + 10y - 25 \\= 9x^2 - (y^2 - 10y + 25) \\= 9x^2 - (y - 5)^2 \\= (3x + y - 5)(3x - y + 5)\end{aligned}$	✓ grouping/groepering ✓ factorising/faktorisering ✓ answer/antwoord (3)
1.2.1	$\begin{aligned}\left(4 + \frac{1}{x}\right)\left(2 - \frac{3}{x}\right) \\= 4\left(2 - \frac{3}{x}\right) + \frac{1}{x}\left(2 - \frac{3}{x}\right) \\= 8 - \frac{12}{x} + \frac{2}{x} - \frac{3}{x^2} \\= 8 - \frac{10}{x} - \frac{3}{x^2}\end{aligned}$	✓ expansion/uitbreiding ✓ answer/antwoord (2)
OR/OF		
	$\begin{aligned}\left(4 + \frac{1}{x}\right)\left(2 - \frac{3}{x}\right) \\= \left(\frac{4x+1}{x}\right)\left(\frac{2x-3}{x}\right) \\= \frac{4x^2 - 12x + 2x - 3}{x^2} \\= \frac{8x^2 - 10x - 3}{x^2}\end{aligned}$	✓ multiplication ✓ answer/antwoord (2)

1.2.2	$\begin{aligned} & \frac{5x - 5}{5x} \\ &= \frac{5(x - 1)}{5x} \\ &= \frac{x - 1}{x} \end{aligned}$ <p>OR/OF</p> $\begin{aligned} & \frac{5x}{5x} - \frac{5}{5x} \\ &= 1 - \frac{1}{x} \end{aligned}$	✓ factorising/faktorisering ✓ answer/antwoord (2)
1.2.3	$\begin{aligned} & \frac{3^{x+1} + 3^x}{27 \cdot 3^{-1+x}} \\ &= \frac{3^x \cdot 3 + 3^x}{27 \cdot 3^{-1} \cdot 3^x} \\ &= \frac{3^x(3 + 1)}{3^x \cdot \frac{27}{3}} \\ &= \frac{4}{9} \end{aligned}$ <p>OR/OF</p> $\begin{aligned} & \frac{3^{x+1} + 3^x}{27 \cdot 3^{-1+x}} \\ &= \frac{3^x \cdot 3 + 3^x}{27 \cdot 3^{-1} \cdot 3^x} \\ &= \frac{4 \cdot 3^x}{3^x \cdot \frac{27}{3}} \\ &= \frac{4}{9} \end{aligned}$	✓ separating bases/ <i>skei basisse</i> ✓ common factor/ <i>gemeensklike faktor</i> ✓ answer/antwoord (3)
		✓ separating bases/ <i>skei basisse</i> ✓ addition/ <i>optelling</i> ✓ answer/antwoord (3)
		[13]

QUESTION/VRAAG 2

2.1.1	$2x^2 - 10x = 0$ $2x(x - 5) = 0$ $x = 0 \text{ or } x = 5$	<p style="border: 1px solid black; padding: 5px;">Answer only: full marks</p>	$x = 0 \checkmark$ $x = 5 \checkmark$ (2)
2.1.2	$px - kx = k - p$ $x(p - k) = k - p$ $x = \frac{k - p}{(p - k)}$ $x = -\frac{k - p}{k - p}$ $x = -1$		\checkmark common factor/ <i>gemeenskaplike faktor</i> \checkmark dividing by $(p - k)$ \checkmark answer/antwoord (3)
2.1.3	$2^{\frac{x}{3}} = \frac{1}{128}$ $2^{\frac{x}{3}} = 2^{-7}$ $\frac{x}{3} = -7$ $x = -21$		$\checkmark \frac{1}{2^7}$ or/of 2^{-7} \checkmark equating exponents/ <i>gelykstelling van eksponente</i> \checkmark answer/antwoord (3)
OR/OF	$2^{\frac{x}{3}} = \frac{1}{128}$ $\left(2^{\frac{x}{3}}\right)^3 = (2^{-7})^3$ $2^x = 2^{-21}$ $x = -21$		$\checkmark \frac{1}{2^7}$ or/of 2^{-7} \checkmark raising by exponent 3 \checkmark answer (3)
OR/OF	$2^{\frac{x}{3}} = \frac{1}{128}$ $\frac{1}{2^{\frac{-x}{3}}} = \frac{1}{2^7}$ $-\frac{x}{3} = 7$ $x = -21$		$\checkmark \frac{1}{2^{\frac{-x}{3}}} = \frac{1}{2^7}$ \checkmark equating exponents \checkmark answer (3)
2.2.1	$\frac{x+5}{2} > -2$ $x+5 > -4$ $x > -9$		\checkmark simplification/ <i>vereenvoudiging</i> \checkmark answer (2)

	OR/OF													
	$\frac{x+5}{2} > -2$ $\frac{x}{2} + \frac{5}{2} > \frac{-4}{2}$ $x+5 > -4$ $x > -9$	✓ simplification/ vereenvoudiging ✓ answer (2)												
2.2.2		✓ number line/getallelyn (1)												
2.3	$x(x-3) + y(3-x) = 0$ $x(x-3) - y(x-3) = 0$ $(x-3)(x-y) = 0$ $x = 3 \text{ or } y = x = 3$	✓ change of sign/ verander teken ✓ common factor/ gemeenskaplike faktor ✓ x-value/-waarde ✓ y-value/-waarde (4)												
2.4	<p>Let the number of R50 notes be x/ Laat die getal R50-note x wees.</p> <table border="1" data-bbox="271 944 1017 1184"> <thead> <tr> <th></th> <th>Number of notes <i>Getal note</i></th> <th>Total value of money/<i>Totale warade van geld</i></th> </tr> </thead> <tbody> <tr> <td>R10</td> <td>$x + 15$</td> <td>$10(x+15)$</td> </tr> <tr> <td>R20</td> <td>$2x$</td> <td>$20(2x)$</td> </tr> <tr> <td>R50</td> <td>x</td> <td>$50(x)$</td> </tr> </tbody> </table> <p> $10(x+15) + 20(2x) + 50x = 10150$ $100x = 10000$ $x = 100$ R10 Notes : $100 + 15 = 115$ R20 Notes : $2(100) = 200$ R50 Notes : $100 = 100$ </p>		Number of notes <i>Getal note</i>	Total value of money/ <i>Totale warade van geld</i>	R10	$x + 15$	$10(x+15)$	R20	$2x$	$20(2x)$	R50	x	$50(x)$	✓ method/metode ✓ simplification/ vereenvoudiging ✓ x-value/-waarde ✓ answer/antwoord R10 notes = 115 R20 notes = 200 R50 notes = 100 (4)
	Number of notes <i>Getal note</i>	Total value of money/ <i>Totale warade van geld</i>												
R10	$x + 15$	$10(x+15)$												
R20	$2x$	$20(2x)$												
R50	x	$50(x)$												
		[19]												

QUESTION/VRAAG 3

3.1.1	$5x + 7$	✓ answer/antwoord (1)
3.1.2	$T_n = mn + c$ $T_n = (x + 2)n + q$ $4x + 5 = xn + 2n + q$ $4x + 5 = 3x + 6 + q$ $x - 1 = q$ $\therefore T_n = (x + 2)n + (x - 1)$	✓ $m = (x + 2)$ ✓ $q = (x - 1)$ ✓ answer/antwoord (3)
	OR/OF	
	$T_0 = 2x + 1 - (x + 2) = x - 1$ $T_n = dn + T_0$ $T_n = (x + 2)n + (x - 1)$	✓ $T_0 = (x - 1)$ ✓ $d = (x + 2)$ ✓ answer/antwoord (3)
	OR/OF	
	For $n = 1$: $(1 + 1) + (2(1) - 1)$ $n = 2$: $(2 + 1) + (2(2) - 1)$ $n = 3$: $(3 + 1) + (2(3) - 1)$ $T_n = (n + 1)x + (2n - 1)$ $T_n = xn + 2n + x - 1$	✓✓ investigating/ ondersoek ✓ answer/antwoord (3)
3.1.3	$T_{13} = 95$ $95 = 13x + 2(13) + x - 1$ $95 = 13x + 26 + x - 1$ $14x = 70$ $x = 5$	✓ substitution/vervanging/ vervanging ✓ answer/antwoord (2)
3.1.4	$T_n = 5n + 2n + 5 - 1$ $T_n = 7n + 4$ $7n + 4 < 158$ $7n < 154$ $n < 22$ \therefore The largest value of n is 21.	✓ $7n + 4 < 158$ ✓ $n < 22$ ✓ conclusion/gevolgtrekking (3)

3.2.1	Height/ Hoogte = 50×44 = 2200 cm	✓ answer/antwoord (1)
3.2.2	$T_n = -0,1n + c$ $T_1 = 7,9$ $7,9 = -0,1 + c$ $\therefore c = 8$ $T_n = -0,1n + 8$ $T_{45} = -0,1(45) + 8$ $T_{45} = 3,5m$ <p>OR/OF</p> $T_n = -10n + c$ $T_1 = 790$ $790 = -10 + c$ $\therefore c = 800$ $T_n = -10n + 800$ $T_{45} = -10(45) + 800$ $T_{45} = 350cm$ $T_{45} = 3,5m$	✓ constant difference/ konstante verskil ✓ T_n ✓ answer/antwoord (3)
	$7,9; 7,8; 7,7; \dots$ $7,9 = -0,1 \times 1 + 8 \dots \dots \dots (1)$ $7,8 = -0,1 \times 2 + 8 \dots \dots \dots (2)$ $7,7 = -0,1 \times 3 + 8 \dots \dots \dots (3)$ $T_n = -0,1 \times n + 8$ $T_n = -0,1n + 8$ $T_{45} = -0,1 \times 45 + 8$ $T_{45} = 3,5m$	✓ general term/algemene term ✓ substitution/vervanging ✓ answer/antwoord (3)
3.2.3	Area of Trapezium/ Oppervlakte van trapesium = $\frac{1}{2}(AB + CD)H$ $= \frac{1}{2}(7,9 + 3,5)22$ $= 125,4 \text{ m}^2$	✓ formula/formule ✓ substitution/vervanging ✓ answer/antwoord (3)

	OR/OF	
	$\begin{aligned} \text{Area of rectangle} &= L \times B \\ &= 7,9 \times 22 \\ &= 173,80 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of TWO right angled triangles} &= 2 \times \frac{1}{2} \times \text{base} \times \text{height} \\ &= 2 \times \frac{1}{2} \times 2,2 \times 22 \\ &= 48,40 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of trapezium} &= 173,80 \text{ m}^2 - 48,40 \text{ m}^2 \\ &= 125,4 \text{ m}^2 \end{aligned}$	✓ area of rectangle ✓ areas of triangles ✓ answer (3)
	OR/OF	
	$\begin{aligned} \text{Area of rectangle} &= L \times B \\ &= 3,5 \times 22 \\ &= 77 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of TWO right angled triangles} &= 2 \times \frac{1}{2} \times \text{base} \times \text{height} \\ &= 2 \times \frac{1}{2} \times 2,2 \times 22 \\ &= 48,40 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of trapezium} &= 77 \text{ m}^2 + 48,40 \text{ m}^2 \\ &= 125,4 \text{ m}^2 \end{aligned}$	✓ area of rectangle ✓ areas of triangles ✓ answer (3)
	OR/OF	
	$\begin{aligned} \text{Area of triangle ADC} &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times 3,5 \times 22 \\ &= 38,5 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of triangle ABC} &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times 7,7 \times 22 \\ &= 86,9 \text{ m}^2 \end{aligned}$ $\begin{aligned} \text{Area of trapezium} &= 38,5 \text{ m}^2 + 86,9 \text{ m}^2 \\ &= 125,4 \text{ m}^2 \end{aligned}$	✓ area of triangle ADC ✓ areas of triangle ABC ✓ answer (3)

[16]

QUESTION/VRAAG 4

4.1.1	$\text{Deposit} = \frac{25}{100} \times R7950 = R1987,50$ $\text{Balance} = R7950 - R1987,50$ $= R5962,50$ <p>OR/OF</p> $\text{Balance} = \frac{75}{100} \times R7950 = R5962,50$	✓ deposit/deposito ✓ balance/balans (2) ✓ 75% ✓ answer/antwoord (2)
4.1.2	$A = P(1 + in)$ $A = R5962,50 \left(1 + \frac{15}{100} \times 2\right)$ $A = R7751,25$ $\text{Monthly payment} = \frac{R7751,25}{24} + R70,75$ $= R393,72$	✓ substitution/vervanging ✓ dividing by 24/deel deur 24 ✓ adding insurance/voeg versekering by ✓ answer/antwoord (4)
4.2.1	$\text{£}55 \times R23,43$ $= R1288,65$	✓ answer/antwoord (1)
4.2.2	<p>Cost of car from England (in rands):</p> $= \text{£}3500 \times R23,43$ $= R82005$ <p>Cost of car from US (in rands):</p> $= \$5500 \times R14,58$ $= R80190$ <p>∴ Car is more expensive in England /Motor is duurder in Engeland</p> <p>OR / OF</p> <p>Cost of a car/Koste van 'n motor</p> $= \frac{5500}{23,43} \times 14,58$ $= \text{£}3 422,54$ <p>∴ Car is more expensive in England /Motor is duurder in Engeland</p> <p>OR/OF</p> <p>Cost of a car/Koste van motor</p> $= \frac{23,43}{14,58} \times 3500$ $= \$5624,49$ <p>∴ Car is more expensive in England /Motor is duurder in Engeland</p>	✓ R82005 ✓ R80190 ✓ conclusion/gevolg-trekking (3) ✓ $\frac{5500}{23,43} \times 14,58$ ✓ £3 422,54 ✓ conclusion/gevolg-trekking (3) ✓ $\frac{23,43}{14,58} \times 3500$ ✓ \$5624,49 ✓ conclusion/gevolgtrekking (3)

[10]

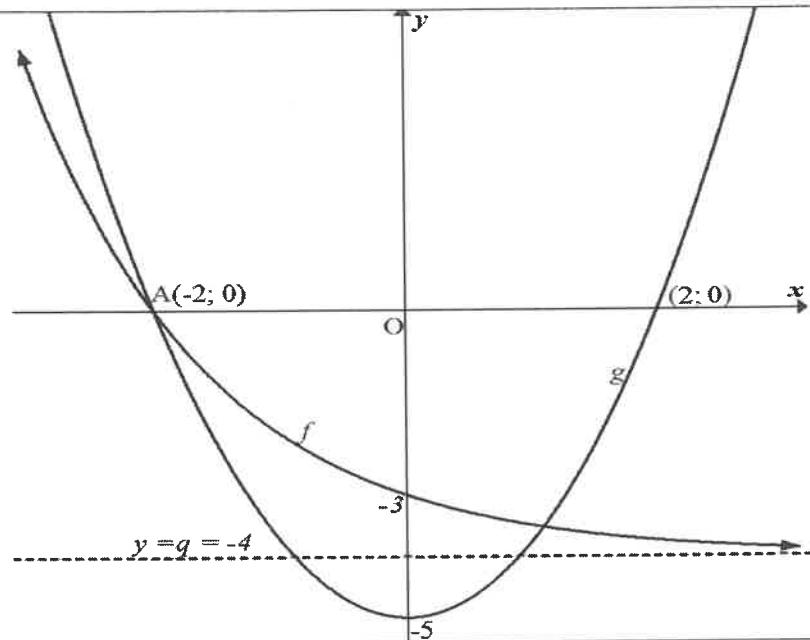
QUESTION/VRAAG 5

5.1.1	$q = 1$	✓ answer/antwoord (1)
5.1.2	$x \in \mathfrak{R}; x \neq 0$ OR/OF $x \in (-\infty; 0) \cup (0; \infty)$	✓ $x \in \mathfrak{R}$ ✓ $x \neq 0$ (2) ✓ ✓ answer/antwoord (2)
	OR/OF $x \in (-\infty; \infty); x \neq 0$	✓ $x \in (-\infty; \infty)$ ✓ $x \neq 0$ (2)
5.2.1	$y = -x + 1$	✓ c value ✓ equation with negative gradient (2)
5.2.2	$x + 2 = 0$ $x = -2$ $0 = \frac{k}{-2} + 1$ $k = 2$ $\therefore f(x) = \frac{2}{x} + 1$	✓ $x = -2$ ✓ substitution $(-2; 0)$ ✓ $k = 2$ ✓ equation/vergelyking (4)
5.2.3	$f(x) = g(x)$ $\frac{2}{x} + 1 = x + 2$ $2 + x = x^2 + 2x$ $x^2 + x - 2 = 0$ $(x + 2)(x - 1) = 0$ $\therefore x = -2 \text{ or } x = 1$ at A : $x = 1 ; y = 3$ A(1; 3)	✓ equating/vergelyking ✓ standard form/ standaardvorm ✓ factorising/ faktorisering ✓ x-values/-waardes ✓ answer/antwoord (5)
		[14]

QUESTION/VRAAG 6

6.1.1	$y = -4$	✓ answer/antwoord (1)
6.1.2	$q = -5$	✓ answer/antwoord (1)
6.1.3	$(2; 0)$	✓ answer/antwoord (1)
6.2.1	$g(x) = ax^2 - 5$ $(-2; 0): 0 = a(-2)^2 - 5$ $0 = 4a - 5$ $a = \frac{5}{4}$ $\therefore g(x) = \frac{5}{4}x^2 - 5$	✓ value of a ✓ equation/vergelyking/ waarde van 'n vergelyking (2)
	OR/OF	
	$g(x) = ax^2 - 5$ $(2; 0): 0 = a(2)^2 - 5$ $0 = 4a - 5$ $a = \frac{5}{4}$ $\therefore g(x) = \frac{5}{4}x^2 - 5$	✓ value of a ✓ equation/vergelyking/ waarde van 'n vergelyking (2)
6.2.2	$f(x) = k^x - 4$ $(-2; 0): 0 = k^{-2} - 4$ $0 = \frac{1}{k^2} - 4$ $4k^2 = 1$ $k^2 = \frac{1}{4}$ $k = \frac{1}{2}$ $\therefore f(x) = \left(\frac{1}{2}\right)^x - 4$	✓ substitution (-2; 0) ✓ value of k / waarde van k ✓ equation/vergelyking (3)
6.3	$y = \left(\frac{1}{2}\right)^0 - 4$ $y = -3$	✓ substitution/vervanging ✓ answer/antwoord (2)

6.4

*f:*

- ✓ asymptotes of/asimptote van f
- ✓ y -intercept of/ y -afsnitte van f
- ✓ shape of/vorm van f

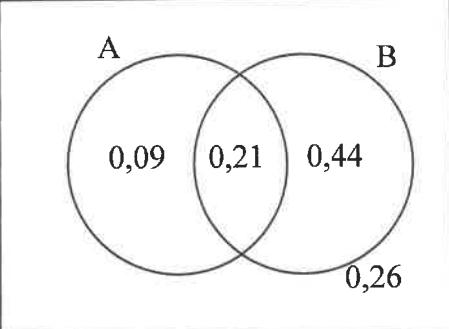
g:

- ✓ x -intercepts/x-afsnitte
- ✓ y -intercept / y -afsnitte
- ✓ shape of/vorm van g

(6)

[16]

QUESTION/VRAAG 7

7.1.1	$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ $0,74 = 0,30 + 0,65 - P(A \text{ and } B)$ $P(A \text{ and } B) = 0,21$	✓ substitution/vervanging ✓ answer/antwoord (2)
7.1.2		✓ 0,09 ✓ 0,21 ✓ 0,44 ✓ 0,26 (4)
7.1.3	No ; $P(A \text{ and } B) \neq 0$ OR/OF No. There is an intersection.	✓ No/Nee ✓ reason/rede (2) ✓ No/Nee ✓ reason/rede (2)
7.2.1	$n(S) = 12$ $n(\text{square no.}) = 3 \text{ (i.e } 1; 4; 9)$ $P(\text{square no.}) = \frac{3}{12}$ $= \frac{1}{4} = 0,25 = 25\%$	✓ answer/antwoord (1)
7.2.2	$P(\text{sum of the 2 numbers} = 2) = \frac{1}{144}$ $P(\text{sum of the 2 numbers greater than } 2) = 1 - \frac{1}{144}$ $= \frac{143}{144}$ $= 0,99$ $= 99\%$	✓ $\frac{1}{144}$ ✓ Complementary rule/ <i>Komplementêre reël</i> ✓ answer/antwoord (3)
		[12]
	TOTAL/TOTAAL:	[100]